

Agent_Zero and Integrative Economics

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Affiliations

- Mathematical and Computational Social Scientist
- Professor of Epidemiology, New York University
 - Affiliated Appointments to the Department of Politics and the Courant Institute of Mathematical Sciences
- Director, the NYU Agent-Based Modeling Lab
- External Professor, Santa Fe Institute

Three Intertwined Endeavors

- Epistemological:
 - Articulated the notion of a *generative explanation* of social phenomena
- Methodological:
 - Developed with others the main *scientific instrument* of generative social science: the Agent-Based Model
 - Recently developed a cognitively plausible alternative to the rational actor—*Agent_Zero*--with which to populate ABMs
- Applied:
 - Have applied *the method of agents* to economics, game theory, epidemiology, environment, archaeology, networks, conflict...
 - Including several collapses (e.g., the ancient Anasazi civilization)

A Trilogy of Books on Agent-Based Modeling

- Epstein and Axtell, *Growing Artificial Societies: Social Science from the Bottom Up* (MIT Press, 1996).
 - Exploratory
 - Immature Epistemology
- Epstein, *Generative Social Science: Studies in Agent-Based Computational Modeling* (Princeton Press, 2006).
 - Explanatory
 - Mature Epistemology
- Epstein, *Agent Zero: Toward Neurocognitive Foundations for Generative Social Science* (Princeton Press, 2013/4)
 - Cognitively plausible agent as foundation for generative explanations
 - Extensions in Epstein and Chelen, “Advancing Agent Zero,” in Wilson and Kirman, eds. *Complexity and Evolution: Toward a New Synthesis for Economics* (MIT Press, 2016)

Specific Topics Today

- Coupled contagions
 - Of some fundamental process (e.g., COVID-19) and fear about it.
 - How their interactions produce volatile dynamics.
- *Agent_Zero* as a foundation for generative social science.
- Several new directions (extensions of *Agent_Zero*, iGSS)

Contagion as a mechanism

- Many economists talk about contagion.
 - Please reread Charles Kindleberger's classic *Manias, panics and crashes: A history of financial crisis*. (1967/2005)
- But, since I play an epidemiologist at NYU, let's start with a simple ABM of an epidemic.
- Core insights emerge even in the Toy model.

“Toy” Playground Epidemic



First Point

- Epidemics are nonlinear...they start out small and then explode.
- So how do you avoid the explosion?

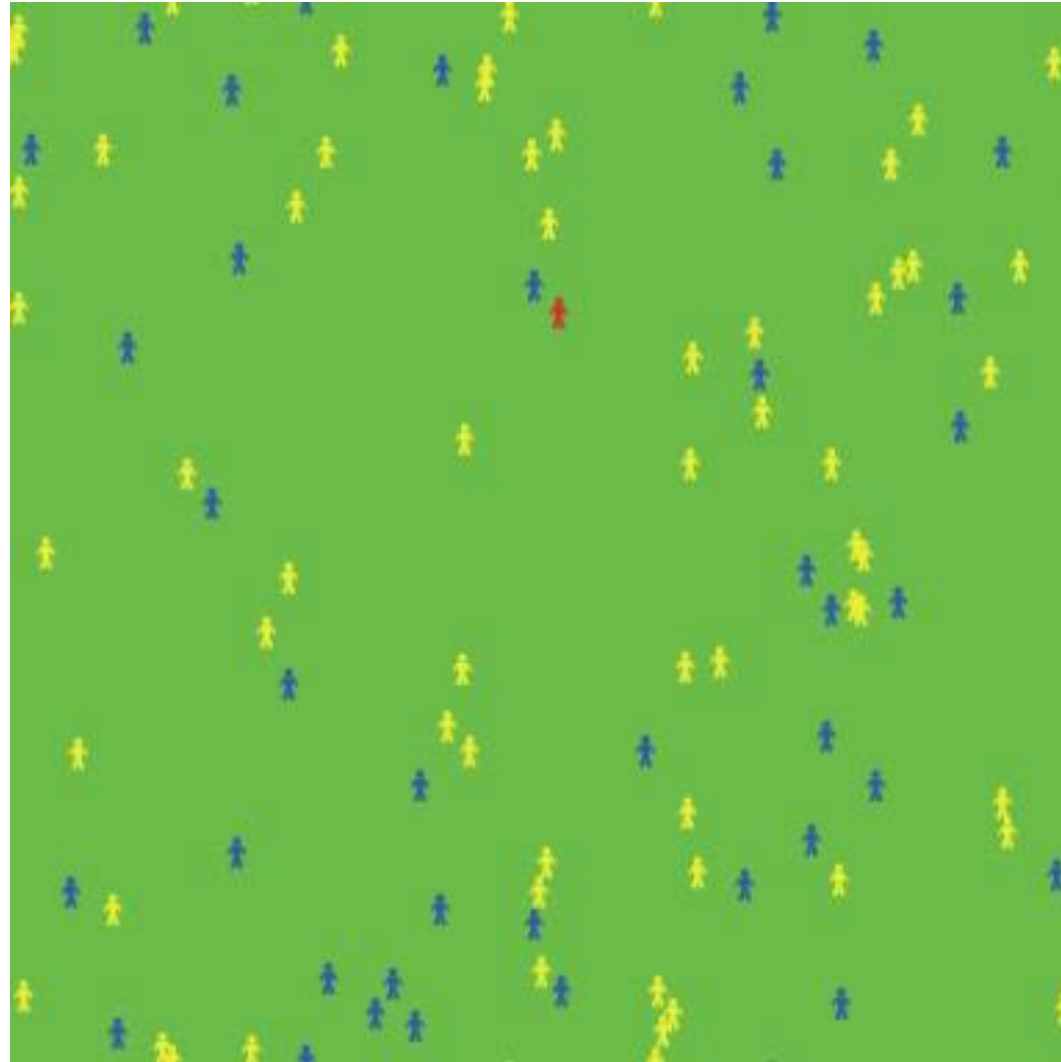
One Approach is Vaccination

- Back to the original run.
- 100 kids. Everybody got it and they all died.
- Now imagine a perfect vaccine.
- Vaccinate 60 kids up front.
- OK...60 survive, yes?

Here's the start: →

If vaccination protected ONLY the vaccinees (yellow), then the only kids alive at the end would be yellow.

Here's what happens:



Herd Immunity!

- More than 60 survive. So, I don't have to immunize everyone to quash the epidemic!
- Just enough so that it fizzles out. OK, so what fraction of the population has to be vaccinated?
- To a first approximation,

$$v > 1 - \frac{1}{?}$$

- What's the one parameter that's all over the news?

You Guessed It : R_0 !

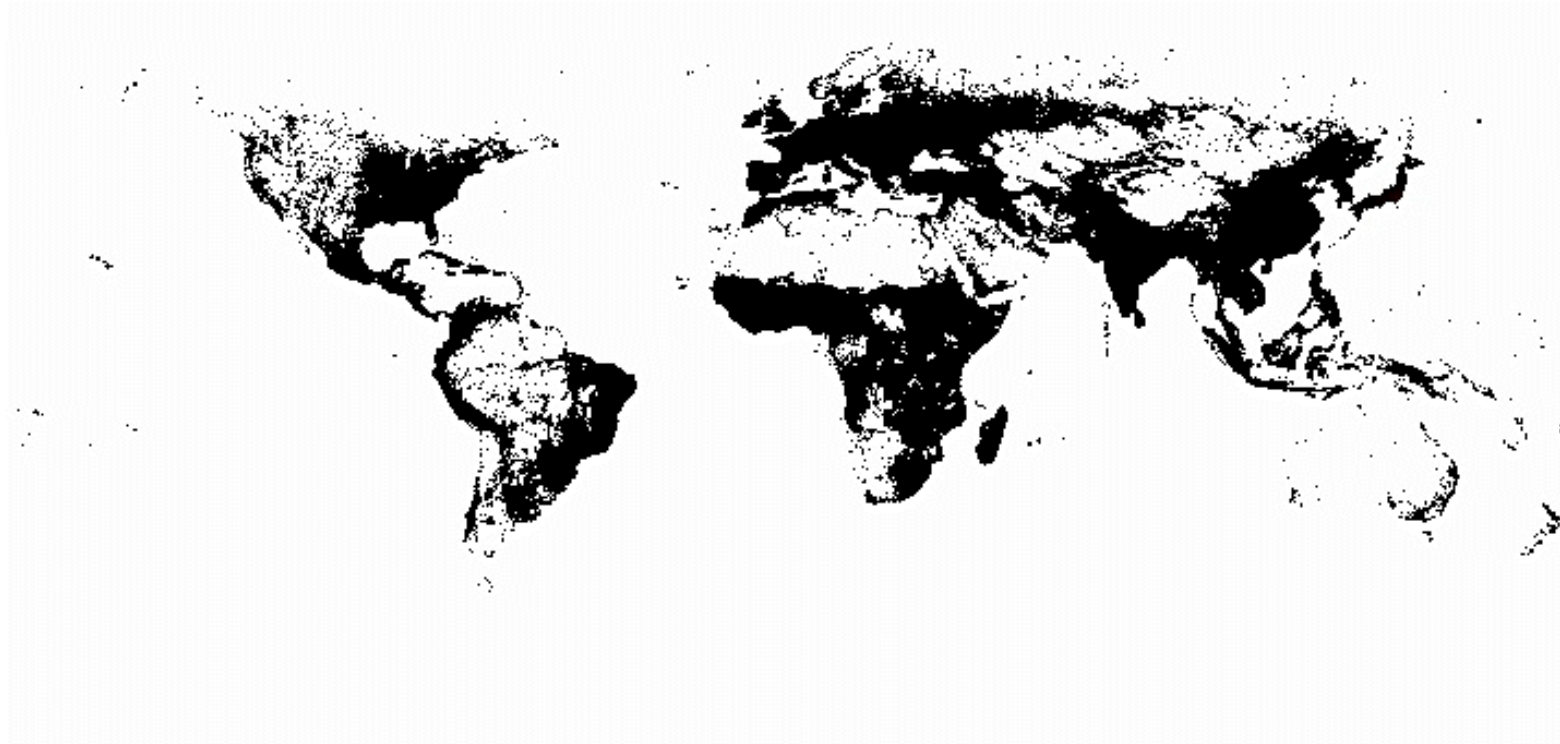
$$v > 1 - \frac{1}{R_0}$$

So, if $R_0 = 2$, you have to (pre) vaccinate $1 - \frac{1}{2} = \frac{1}{2}$ the population... or get them out of harm's way through: household isolation, school and workplace closures (social distancing), cancelation of mass events, restrict international travel, aggressive testing, other measures

Lo and Behold....

- Corona Virus COVID-19: $R_0 \approx 2$ (as was the 1918 Spanish Flu)
- Had China pre-vaccinated—or *effectively isolated*--half of the susceptible pool, they might have nipped it in the bud.
- China was too late and the Wuhan *cordon-sanitaire* alone does not do this. It builds a *wall around* the playground, but does not segregate susceptible and infected populations within it.
- They instituted draconian isolation measures ('hospitals') and it has just turned around through saturation and distancing.
- But many cats had left the bag...and things move quickly these days.

Global-Scale Agent Model (GSAM) 6.5 Billion Agents



Epstein, *Nature*, 2009.

Parker and Epstein, *TOMACS*, 2011

Coupled Contagion

- Of course, what we are seeing today is a coupled contagion.
- One contagion is true disease.
- The other is fear of disease, which affects both health behavior and economic behavior
- We have a model of coupled contagion, based on:

The Classic SIR Model (1927), Playground Version above

- Rates of change of the susceptible, infective, and removed pools

$$\frac{dS}{dt} = -\beta SI . \text{ Falling because leaving } S \text{ for } I \text{ pool}$$

$$\frac{dI}{dt} = \beta SI - \gamma I . \text{ Filling from } S, \text{ but draining to } R$$

$$\frac{dR}{dt} = \gamma I$$

OK, so when is the infective level growing (dI/dt positive)?

That's when more comes in (βSI) than goes out (γI) right?

Herd Immunity

Infected pool expanding when

$$\frac{dI}{dt} > 0 \rightarrow \beta SI - \gamma I > 0 \rightarrow \beta SI > \gamma I.$$

So we have the threshold condition, or tipping point :

Growing if [1] $S > \frac{\gamma}{\beta}$

Fading Out if [2] $S < \frac{\gamma}{\beta}$

Crucial : Don't have to immunize everybody. Just until the susceptibles are sub - threshold

This is called *Herd Immunity*...to infection, financial panic, mob violence.

Recast in Terms of Famous R_0

$$R_0 \equiv \frac{\beta S_0}{\gamma}$$

Interpretation: net secondary infections for one index

$R_0 > 1 \Rightarrow$ epidemic

$R_0 < 1 \Rightarrow$ none

For Financial Panics

- What is the R_0 of contagious fear?
- What constitutes “immunization” from it?
- What is the optimal “vaccination” pattern?

- As Integrative Economists, we care about interactions...

Economic Response to COVID-19 a Coupled Contagion

- One of disease and one of *fear*.
- We published a model of that.

Coupled Contagion Dynamics of Fear and Disease: Mathematical and Computational Explorations (Epstein et al, 2008 Plos_ONE)

- Two interacting contagion processes: one of disease one of *fear about* the disease.
- Individuals contract disease only through contact with the disease-infected (the sick).
- Individuals contract fear through contact with the disease-infected (the sick), the fear-infected (the scared), and those infected with both fear and disease (the sick and scared).
- Scared individuals--whether sick or not--withdraw from circulation with some probability, which affects the course of the disease epidemic proper.
- If individuals recover from fear and return to circulation, the disease dynamics become rich, and include multiple waves of infection, such as occurred in the 1918 flu.
- Recent work on this using Twitter Data (Broniatowski, et al, 2016).

Possible states

S: Susceptible to pathogen and fear
 I_F : Infected with fear only
 I_P : Infected with pathogen only
 I_{PF} : Infected with pathogen and fear
 R_F : Removed from circulation due to fear
 R_{PF} : Removed from circulation due to fear and infected with pathogen
R: Recovered from pathogen and immune to fear

Transmission probabilities

	Get scared (α)	Not get scared
Get Sick (β)	$\alpha \beta$	$(1 - \alpha) \beta$
Not get sick	$\alpha (1 - \beta)$	$(1 - \alpha) (1 - \beta)$

Parameters governing Removal and Return

λ_1 : Rate of removal to self-isolation of those infected with fear only
 λ_2 : Rate of recovery from infection with pathogen
 λ_3 : Rate of removal to self-isolation of those infected with fear and pathogen
H: Rate of recovery from fear and return to circulation

The appropriate generalization is.....

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Financial panic



Parameters governing Removal and Return

λ_1 : Rate of removal to self-isolation of those infected with fear only
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 λ_3 : Rate of removal to self-isolation of those infected with fear and pathogen
 H: Rate of recovery from fear and return to circulation

The appropriate generalization is.....

Classical SIR Differential Equations Formulation

$$\begin{aligned}\frac{dS}{dt} = & -\beta(1-\alpha)SI_P - (1-\beta)\alpha SI_P - \beta\alpha SI_P - \alpha SI_F - \beta(1-\alpha)SI_{PF} \\ & - (1-\beta)\alpha SI_{PF} - \beta\alpha SI_{PF} + HR_F\end{aligned}$$

$$\frac{dI_F}{dt} = (1-\beta)\alpha SI_P + \alpha SI_F + (1-\beta)\alpha SI_{PF} - \beta I_F I_P - \beta I_F I_{PF} - \lambda_1 I_F$$

$$\frac{dI_P}{dt} = \beta(1-\alpha)SI_P + \beta(1-\alpha)SI_{PF} - \alpha I_P I_P - \alpha I_P I_F - \alpha I_P I_{PF} - \lambda_2 I_P + HR_{PF}$$

$$\frac{dI_{PF}}{dt} = \beta\alpha SI_P + \beta\alpha SI_{PF} + \beta I_F I_P + \beta I_F I_{PF} + \alpha I_P I_P + \alpha I_P I_F + \alpha I_P I_{PF} - \lambda_2 I_{PF} - \lambda_3 I_{PF}$$

$$\frac{dR_F}{dt} = \lambda_1 I_{PF} - HR_F$$

$$\frac{dR_{PF}}{dt} = \lambda_3 I_{PF} - \lambda_2 R_{PF} - HR_{PF}$$

$$\frac{dR}{dt} = \lambda_2 I_P + \lambda_2 I_{PF} + \lambda_2 R_{PF}$$

Subsumes Classical Models

With $b=0$, SIR for fear

$$\frac{dS}{dt} = -\beta(1-\alpha)SI_P - (1-\beta)\alpha SI_P - \beta\alpha SI_P - \alpha SI_F - \beta(1-\alpha)SI_{PF} - (1-\beta)\alpha SI_{PF} - \beta\alpha SI_{PF} + HR_F$$

With $a=0$, SIR for pathogen

$$\frac{dI_F}{dt} = (1-\beta)\alpha SI_P + \alpha SI_F + (1-\beta)\alpha SI_{PF} - \beta I_F I_P - \beta I_F I_{PF} - \lambda_1 I_F$$

$$\frac{dI_P}{dt} = \beta(1-\alpha)SI_P + \beta(1-\alpha)SI_{PF} - \alpha I_P I_P - \alpha I_P I_F - \alpha I_P I_{PF} - \lambda_2 I_P + HR_{PF}$$

$$\frac{dI_{PF}}{dt} = \beta\alpha SI_P + \beta\alpha SI_{PF} + \beta I_F I_P + \beta I_F I_{PF} + \alpha I_P I_P + \alpha I_P I_F + \alpha I_P I_{PF} - \lambda_2 I_{PF} - \lambda_3 I_{PF}$$

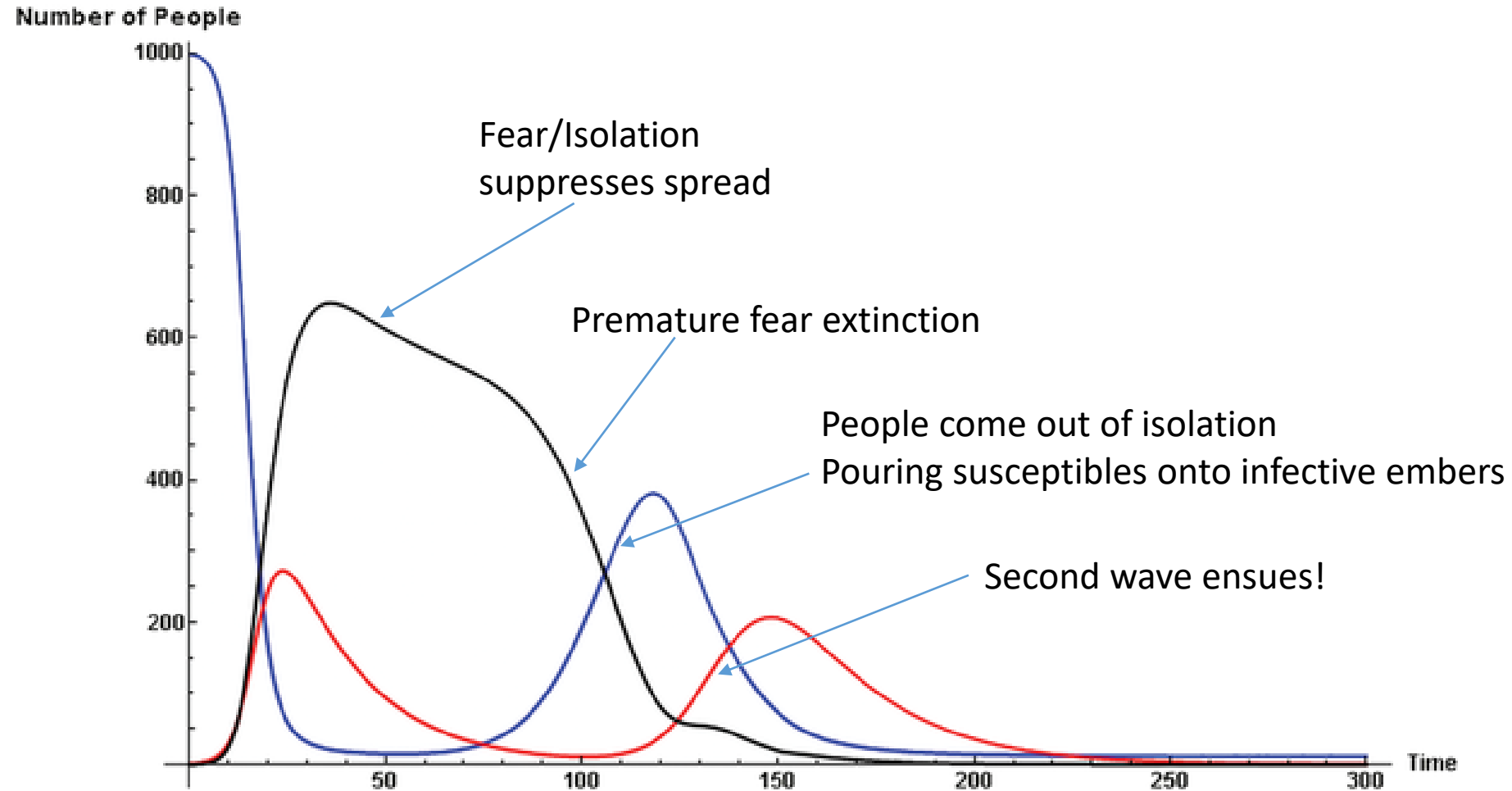
Removals and re-entry to S

$$\frac{dR_F}{dt} = \lambda_1 I_{PF} - HR_F$$

$$\frac{dR_{PF}}{dt} = \lambda_3 I_{PF} - \lambda_2 R_{PF} - HR_{PF}$$

$$\frac{dR}{dt} = \lambda_2 I_P + \lambda_2 I_{PF} + \lambda_2 R_{PF}$$

Figure 3. In the idealized run of figure 3, susceptible individuals (blue-curve) self-isolate (black curve) through fear as the infection of disease proper grows (red curve).

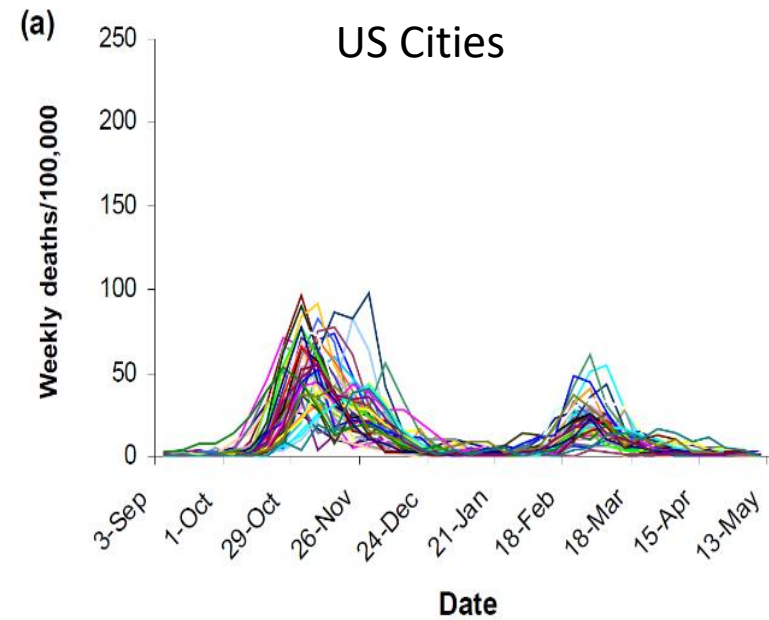
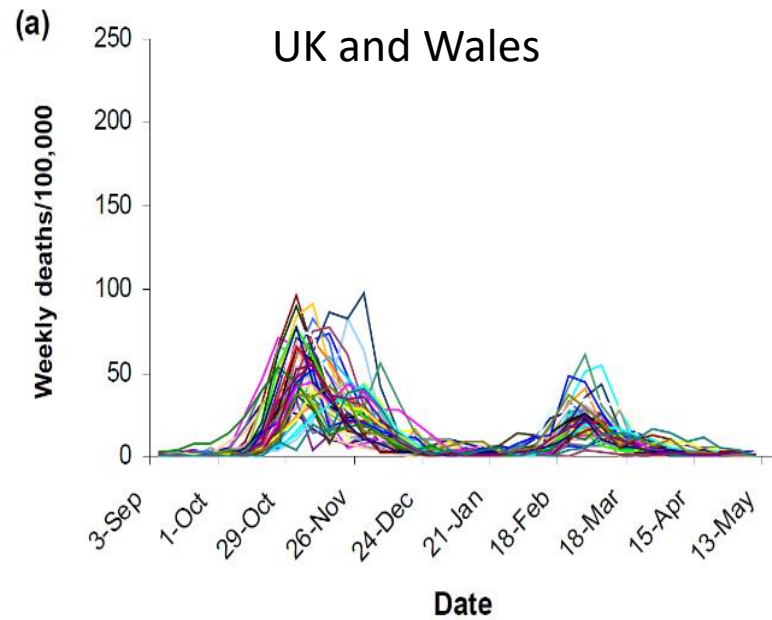


Epstein JM, Parker J, Cummings D, Hammond RA (2008) Coupled Contagion Dynamics of Fear and Disease: Mathematical and Computational Explorations. PLOS ONE 3(12): e3955. <https://doi.org/10.1371/journal.pone.0003955>
<https://journals.plos.org/plosone/article?id=10.1371/journal.pone.0003955>

Main Mystery of 1918 Spanish Flu (50m dead)

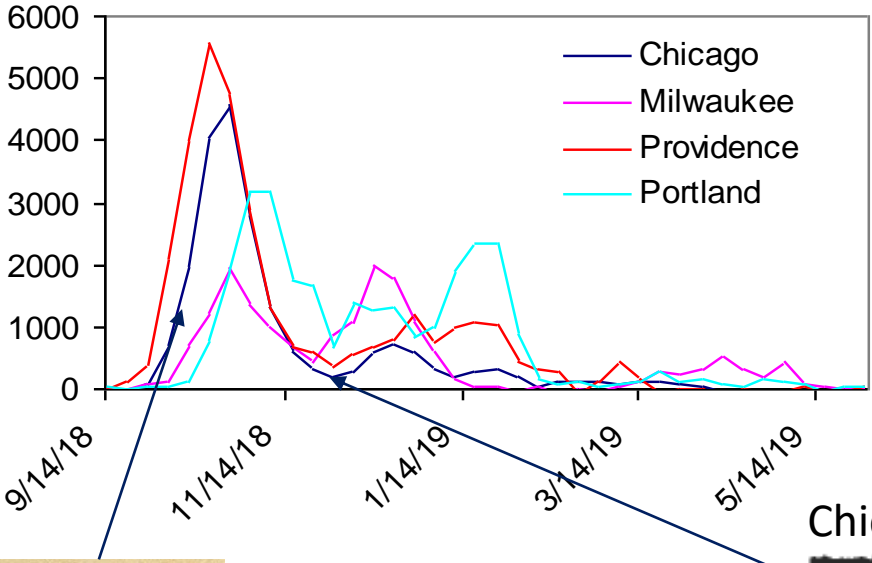
- Multiple waves of infection.
- Here is a behavioral mechanism

Very Crude Qualitative Agreement for Cities



Emboldened, I conducted a massive *big data* analysis for Chicago

Chicago



Chicago Tribune, November 10, 1918

INFLUENZA
 FREQUENTLY COMPLICATED WITH
PNEUMONIA
 IS PREVALENT AT THIS TIME THROUGHOUT AMERICA.
 THIS THEATRE IS CO-OPERATING WITH THE DEPARTMENT OF HEALTH.
YOU MUST DO THE SAME
 IF YOU HAVE A COLD AND ARE COUGHING AND
 SNEEZING. DO NOT ENTER THIS THEATRE
GO HOME AND GO TO BED UNTIL YOU ARE WELL.

Coughing, Sneezing or Spitting Will Not Be Permitted In The Theatre. In case you must cough or Sneeze, do so in your own handkerchief, and if the Coughing or Sneezing Persists Leave The Theatre At Once.

This Theatre has agreed to co-operate with the Department Of Health in disseminating the truth about Influenza, and thus serve a great educational purpose.

HELP US TO KEEP CHICAGO THE HEALTHIEST CITY IN THE WORLD
JOHN DILL ROBERTSON
 COMMISSIONER OF HEALTH

ALL BANS OFF
 Chicago Healthiest City in the World, Says Robertson.

If you want to dodge the "flu" and the "pneu" Chicago is the best place to be in. The epidemic here is over. Dr. John Dill Robertson, commissioner of health, in a letter to Lucius Teter, president of the Chicago Association of Commerce, yesterday declared that, so far as pneumonia and influenza are concerned, Chicago is the safest place in the United States.

"We are practically out of the woods," wrote Dr. Robertson. "All bans are off. In a few days I am sure I shall again be justified in stating that Chicago is the healthiest city in the world."



Adages...

- Einstein, Theory should be “as simple as possible, but no simpler”
- Epstein, Data should be “as big as necessary, but no bigger.”

Fear vs. Bug

- Fear can dissipate before the infection does
- Fear can also transmit faster than the bug itself, even if $\alpha = \beta$ (why?)
 - More channels
 - Does not require physical contact
- Fear faster than bug if:

$$\alpha > \frac{\beta \lambda_1 (\lambda_2 + \lambda_3)}{(\lambda_1 + \lambda_3)(\lambda_2 + \lambda_3) - \beta \lambda_1 \lambda_3}$$

Adapt to Financial Contagion

- Same basic formalism for the contagions proper
- But the removal due to fear would be from the economy (sell-offs).
- It would not feed back to suppress the epidemic as in removal from physical circulation (which could still be in the model).
- Might try to calibrate to the epidemic and market dynamics data, as an Integrative Economics exercise.

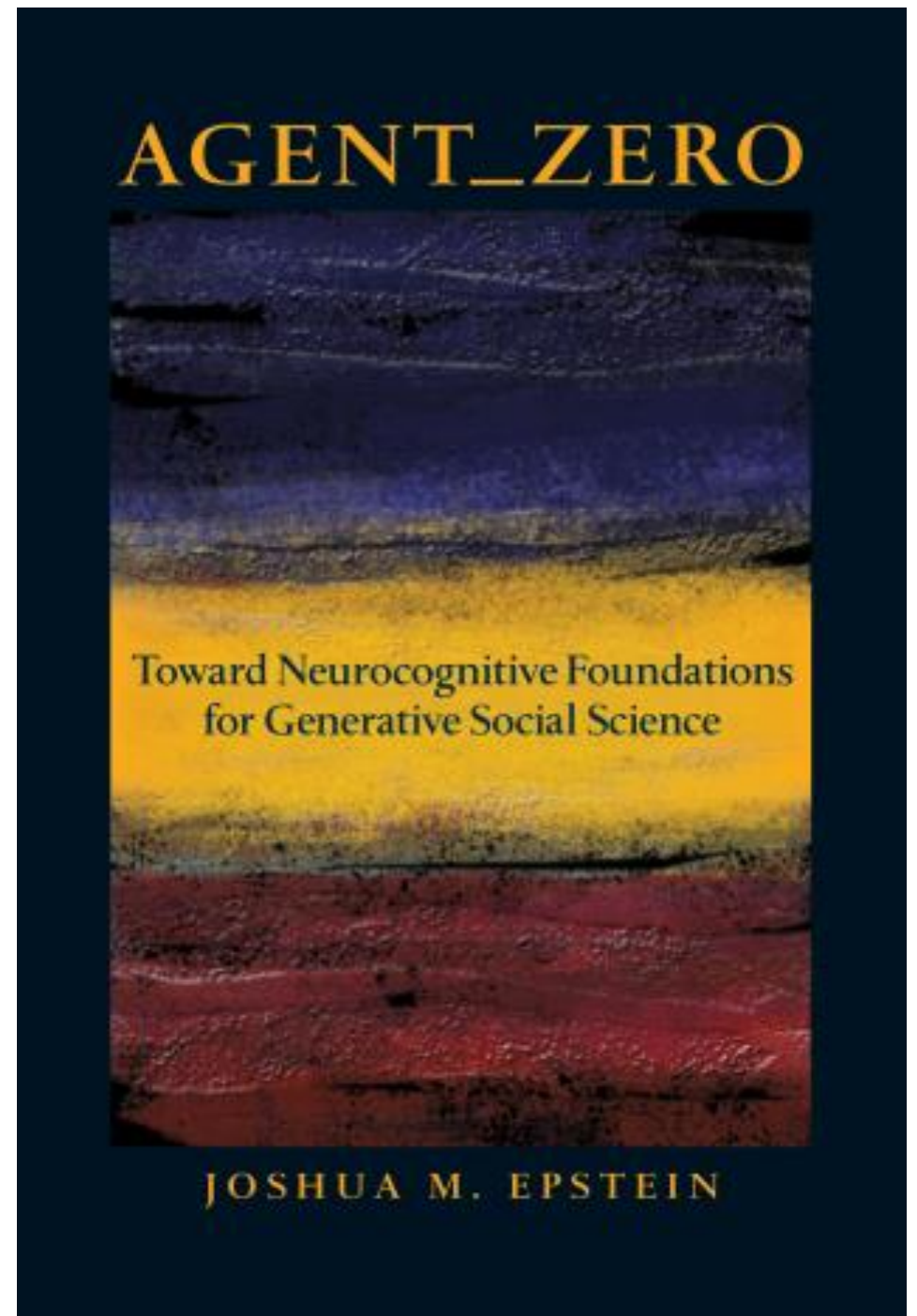
Taking “Fear” Seriously...

- We’ve thrown this term around...all very nice.
- But can treat it more seriously?
- How fear happens, how it evaporates, any neural correlates?

Part II: Agent_Zero

*Agent_Zero: Toward Neurocognitive
Foundations for Generative Social Science
Princeton University Press 2013*

Funded by an NIH Director's Pioneer Award



Generative explanation*

- To explain a social regularity
- Demonstrate how it could emerge on time scales of interest to humans in a population of cognitively plausible agents
- Does the micro-specification m generate the macroscopic *explanandum* x
- If so, m is a generative explanatory candidate.
- Motto (Epstein, 1999) is negative : If you didn't grow it, you didn't explain it.

$$\forall x(\neg Gx \supset \neg Ex)$$

- *Not* the converse (any old way of growing it is explanatory).
- *Not* uniqueness (might be many m 's).
- Generative sufficiency a necessary (but not sufficient) condition for explanation.
- \neg Furnish a Game in which the pattern is Nash
- \neg Furnish a Functional with respect to which the trajectory is an extremal
- \neg Furnish a Regression relating aggregate variables.

* ... as against prediction.

Generative explanation*

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Cognitively Plausible Agents

- Have emotions (notably fear)
- Have bounded deliberative capacity
- Have social connection
- And all of those might matter.
- Accordingly...

Agent_Zero

Endowed with distinct affective, deliberative, and social modules each grounded in contemporary neuroscience:

Internal modules interact to produce observable individual behavior.

Multiple agents interacting generate wide variety of collective dynamics: health, conflict, network dynamics, economics, social psychology, law.

Get synthesis started.

All provisional....

But Formal

Lots of empirical criticisms of the rational actor of Economics and Game Theory.

Gripes (even decisive experiments) do not change scientific practice.

Need explicit formal alternatives.

Albeit provisional, *Agent_Zero* is one: mathematical and computational.

- Before laying out the equations ...

Big Picture...where we're going.

The violence interpretation

- Agents occupy an landscape of indigenous sites.
- There's a binary action agents can take: destroy some sites
- Experience produces a *disposition* to take the binary action
- Some sites are inactive/benign. Some active/fear-inducing
- Affect: Agents fear-condition on local stimuli: NOT decision-making or choosing.
 - Passion
- Bounded rationality: Local sample relative frequency
 - Reason
- Add these. Solo Disposition (propensity to perform the act).
- Social animals: Add others' weighted Solo Dispositions
 - Weights are endogenous (minimize parameters)
- If Total Disposition exceeds threshold, take the action.
 - Destroy, or flee, or refuse vaccine, or dump assets, or find guilty...

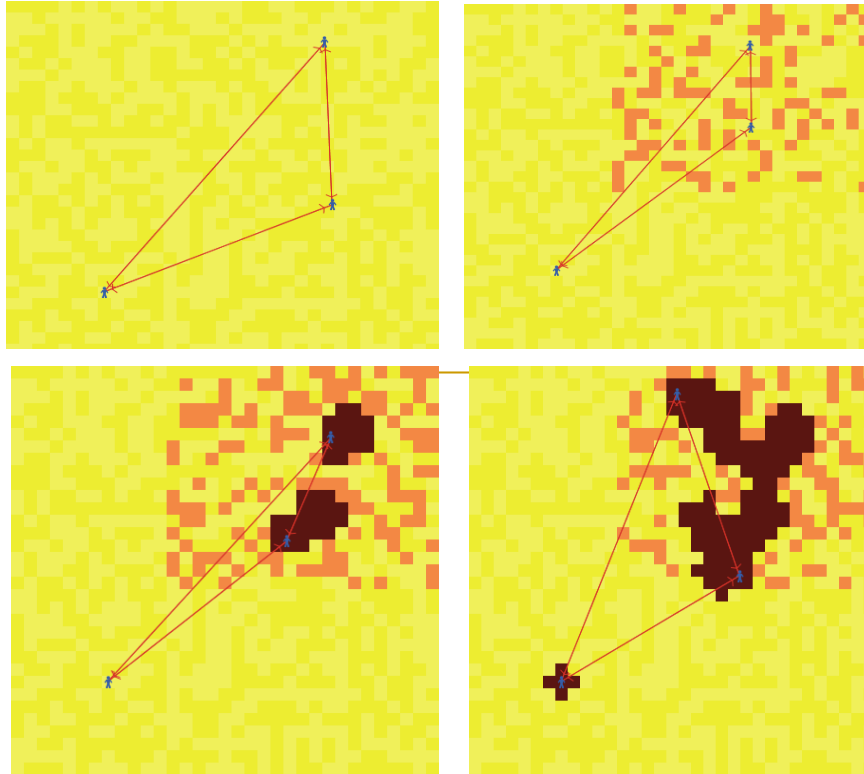
Computational **Parables** : Slaughter of Innocents

Vision Von Neumann

Agent #0 fixed in SW: zero direct stimulus

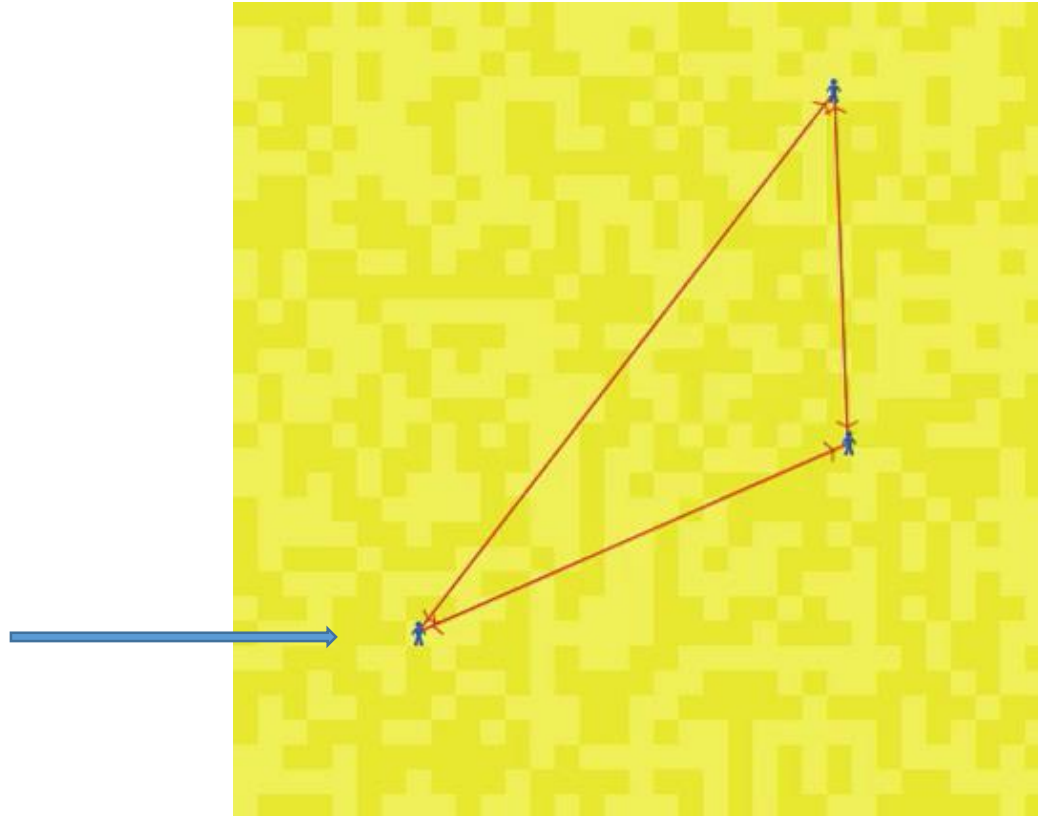
Others in NE: stimulus, violent action

By dispositional contagion, Agent 0 acts.



Parable 1: Agent_Zero Joins Without Direct Stimulus (eye candy runs are just sample paths, of course)

Since no stimulus
within sensory radius.
Would not act alone



Overall Set-Up

Action , Threshold

- Binary Action

- Flee snake or don't
- Raid icebox or don't
- Join lynching or don't
- Refuse vaccine or don't
- Dump stock or don't
- Wipe out village or don't
- "Behavior" will mean a **binary** action.

$$A \in \{0,1\}$$

- Nonnegative Real Threshold

$$\tau \geq 0$$

Solo Disposition to Act

- Agents endowed with Affective $V(t)$ and Deliberative real-valued functions $P(t)$ bounded to $[0,1]$ defined on a stochastic stimulus space, and each Solo disposition is, for the moment, as simple as possible, their sum:

$$D_i^{solo}(t) = V_i(t) + P_i(t)$$

- Addition also nice when they compete given a threshold

But Connected: Total Disposition to Act

- Again, solo disposition is the sum: $D_i^{solo}(t) = V_i(t) + P_i(t)$
- But Agents also carry weights (unconsciously I presume): $\omega_{ji}(t)$
- We therefore define the Total Disposition to Act as*

$$D_i^{tot}(t) = D_i^{solo}(t) + \sum_{j \neq i} \omega_{ji}(t) D_j^{solo}(t)$$

*self-weights assumed to be one, but can relax (low self-esteem agents).

Action Rule

Act if and only if $D_i^{tot}(t) > \tau_i$.

Or, defining $D_i^{net}(t) \equiv D_i^{tot}(t) - \tau_i$,

The Action Rule reduces to :

Act iff $D_i^{net}(t) > 0$.

Dispositional Contagion, Not Imitation of Behavior

- Nobody else's observable *action* appears in this equation.
- Hence, the mechanism of action cannot be imitation of behavior, because the binary acts of others are not registered in this calculation.
- So we are suspending a “monkey-see/monkey-do” assumption central to much literature on social transmission.
- Obvious problem with imitation of observable action: no mechanism for the *first* actor. Nobody to imitate.
- (Noise is cheating...not a mechanism)

Under The Hood: Provisional Parsimonious (Master Class for More)

$$\text{Act if } D_i^{tot}(t) = V_i(t) + P_i(t) + \sum_{j \neq i} \omega_{ji}(t)(V_i(t) + P_i(t)) > \tau_i$$

τ_i 's equal, so one parameter

$$v_i(t) \text{ solves } \frac{dv_i}{dt} = \alpha_i \beta_i v_i^\delta (\lambda - v_i) \text{ Nonlinear Rescorla - Wagner}$$

Original is just $k_i(1 - v_i)$. So also one parameter. Neuroscience coming up.

$$P_i(t, x; m) = \frac{1}{m} \sum_{t-m}^t RF(x) \text{ Moving average of local relative frequency}$$

Memory a third parameter. Weights endogenous

$$\omega_{ji}(t) = [v_i(t) + v_j(t)](1 - |v_i(t) - v_j(t)|) \text{ Strength - scaled affective homophily}$$

Where t meters trials for mobile agents on a spatial stimulus landscape

Humble goal:

- Get the synthesis started
- Provisional plausible/testable modules

ODE (deterministic/non-spatial)
and ABM (stochastic/spatial) versions
(Math and *Mathematica* Code in the book)

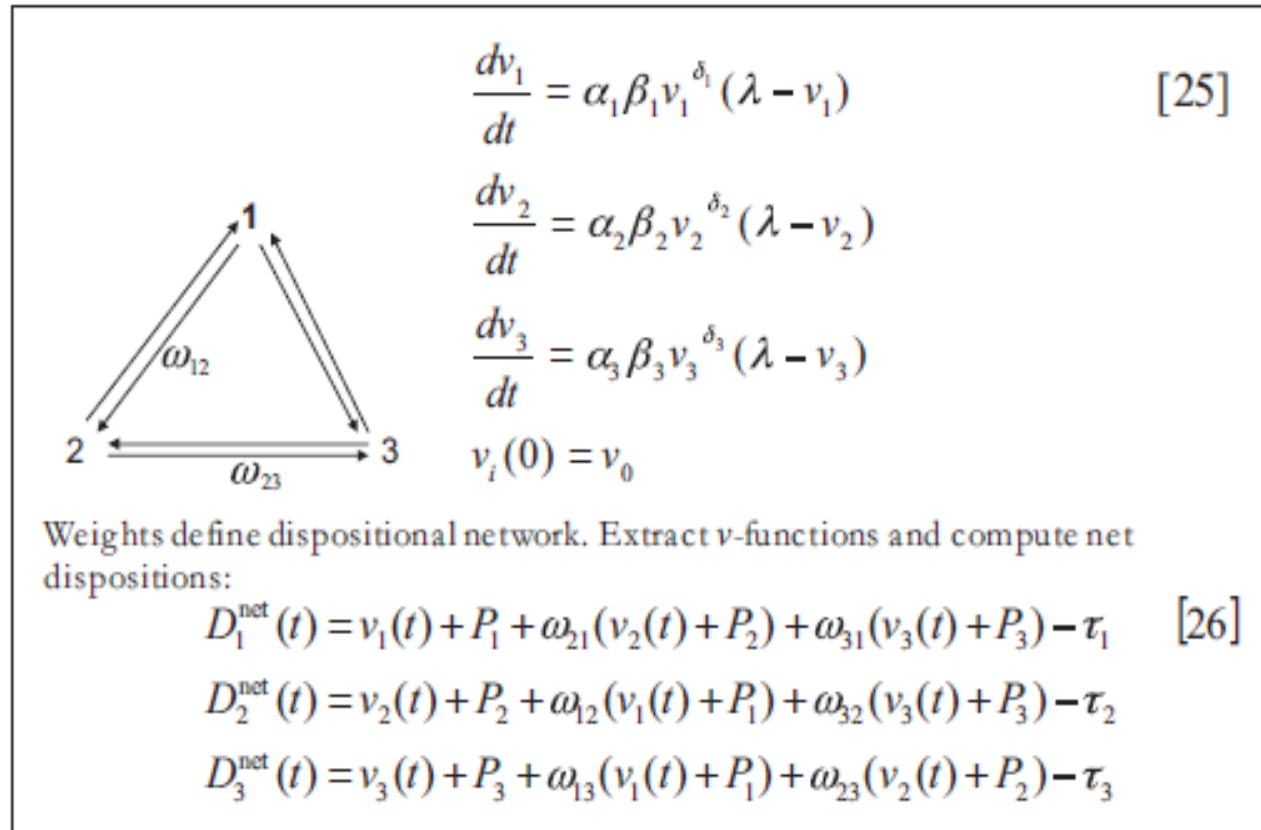


FIGURE 24. Generalized Three-Agent Model

The Subtitle of *Agent_Zero*

- Toward Neurocognitive Foundations for Generative Social Science
- Talked about Generative Social Science
- What's this neurocognitive business?

Fear Instantiation

- Fear acquisition
- Fear extinction

- Now I will butcher some neuroscience...

Amygdala Circuit

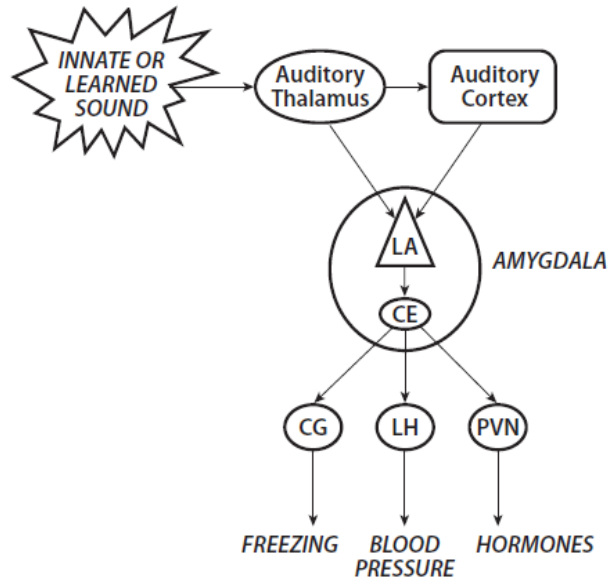


FIGURE 1. Auditory Amygdala Stimuli and Defense Responses. Source: LeDoux (2002, Figure 5.6)

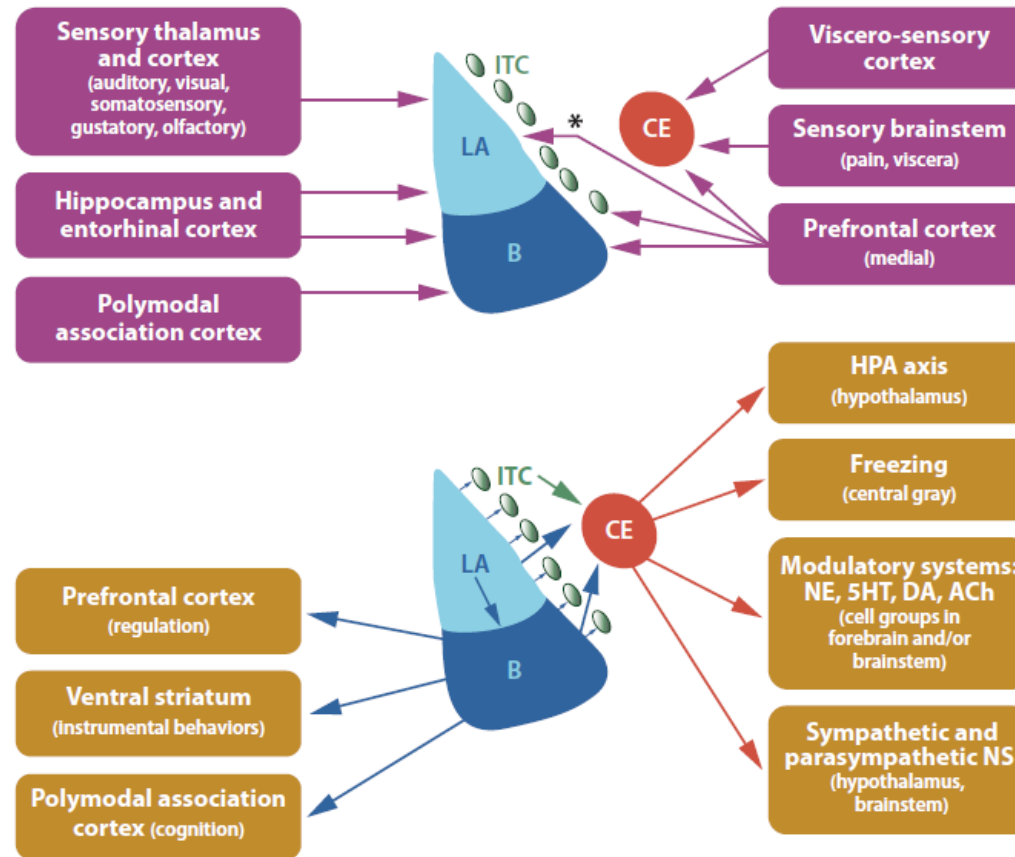


FIGURE 2. Amygdala Inputs and Outputs. Inputs to some specific amygdala nuclei. Asterisk (*) denotes species difference in connectivity. (Bottom) Outputs of some specific amygdala nuclei. 5HT, serotonin; Ach, acetylcholine; B, basal nucleus; CE, central nucleus; DA, dopamine; ITC, intercalated cells; LA, lateral nucleus; NE, nor-epinephrine; NS, nervous system. Source: Rodrigues, LeDoux, and Sapolsky (2009)

Amygdala Areas: Various Stains

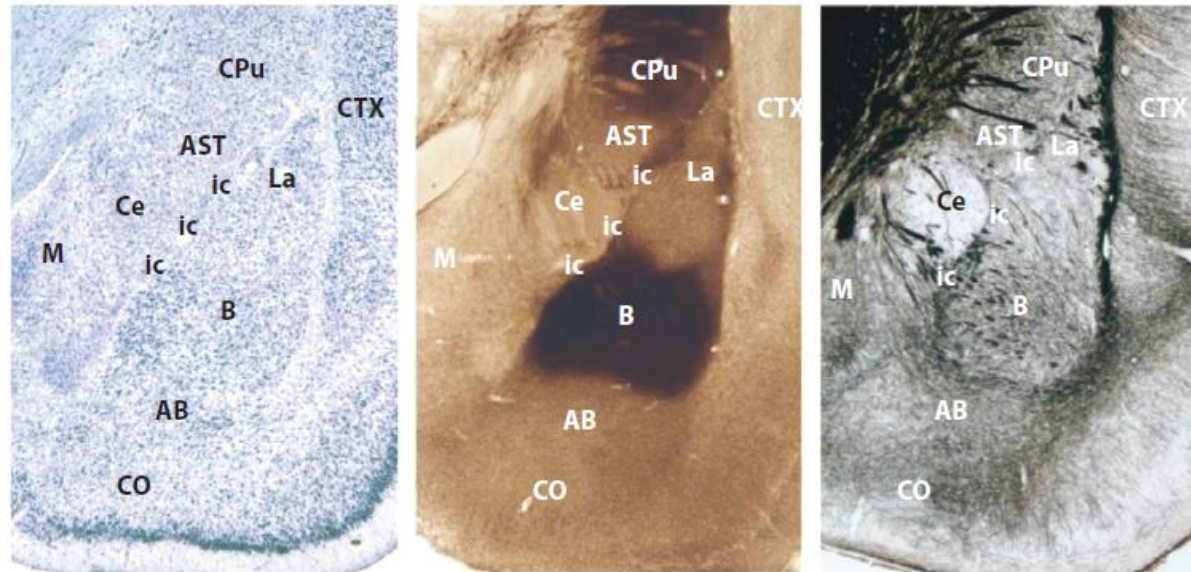


FIGURE 3. Key Areas of the Amygdala. Key areas of the amygdala, as shown in the rat brain. The same nuclei are present in primates, including humans. Different staining methods show amygdala nuclei from different perspectives. Left panel: Nissl cell body stain. Middle panel: acetylcholinesterase stain. Right panel: silver fiber stain. Abbreviations of amygdala areas: AB, accessory basal; B, basal nucleus; Ce, central nucleus; ic, intercalated cells; La, lateral nucleus; M, medial nucleus; CO, cortical nucleus. Non-amygdala areas: AST, amygdalo-striatal transition area; CPu, caudate putamen; CTX, cortex. Source: LeDoux (2008, p. 2698); reprinted courtesy of Joseph E. LeDoux

Don't Care *Where*...Care that it's Innate, Automatic, Fast, Inaccessible to Deliberation

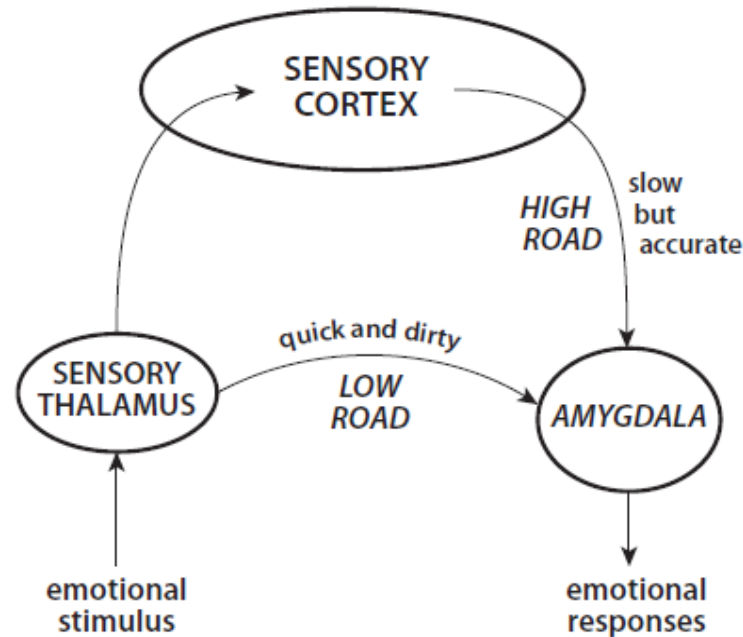


FIGURE 4. Low Road and High Road to Fear. Source: LeDoux (2002, pp. 61–63, Figure 5.7)

Also equipped with an associative machinery.

“Neurons that fire together wire together.” Donald Hebb (1949)

Associative Fear Conditioning: Acquisition Phase

US: Shock cuff

UR: Amygdala activation

CS: Blue Light (neutral)

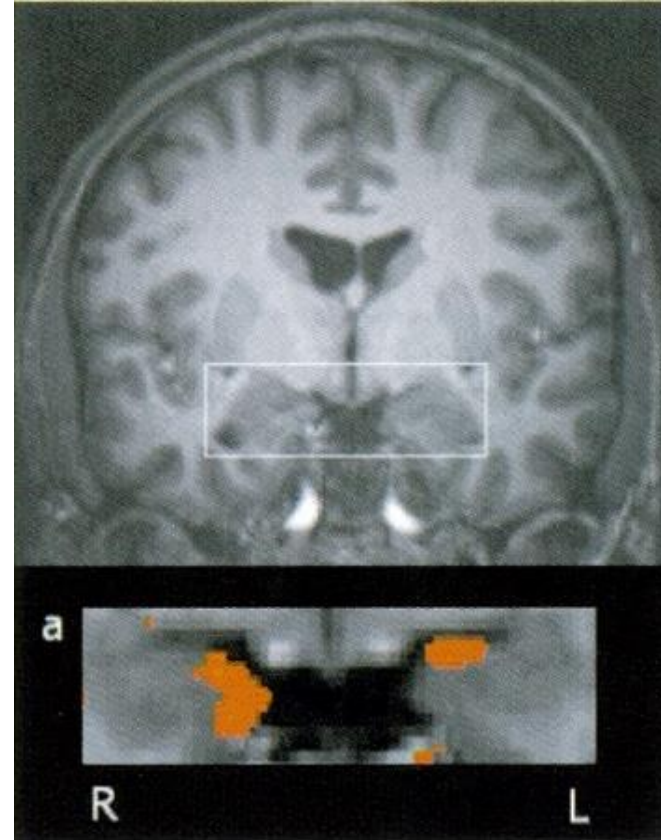
CS-US Pairing Trials

Light...Shock

Light...Shock

Light...Shock

Light alone →



Hume's Association of Ideas

“. . . after the constant conjunction of two objects . . . we are determined by *custom* alone to expect the one from the appearance of the other . . . Having found in many instances, that two kinds of objects—flame and heat, snow and cold—have always been conjoined together; if flame or snow be presented anew to the senses, the mind is carried by *custom* to expect heat or cold.” It is not by reasoning, moreover, that we form the connection.

“All these operations are a species of natural instinct, **which no reasoning or process of the thought and understanding is able either to produce or to prevent**” (Section V, Part I).

Very important: Nonconscious and inaccessible to ratiocination.

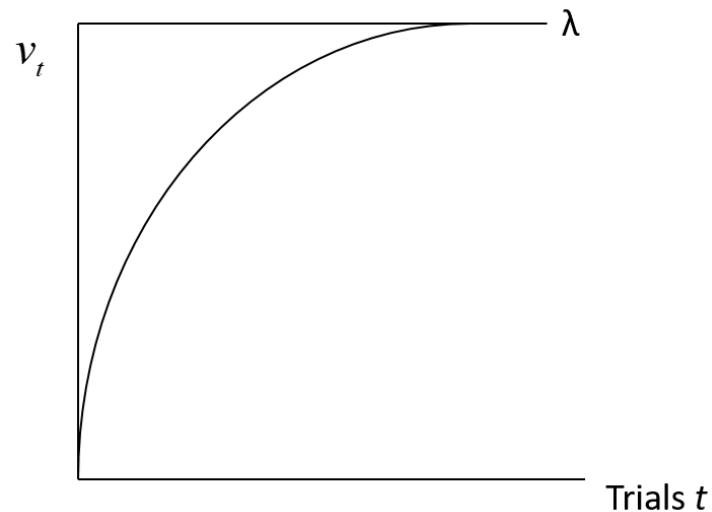
Simple Elegant Model of Associative Learning Rescorla-Wagner Model (1972)

$$v_{t+1} - v_t = \alpha\beta(\lambda - v_t)$$

Learning rates (α, β) : **Surprise and Saliency**

Associative gain requires Surprise and Saliency

λ (typically 1) is max associative strength.

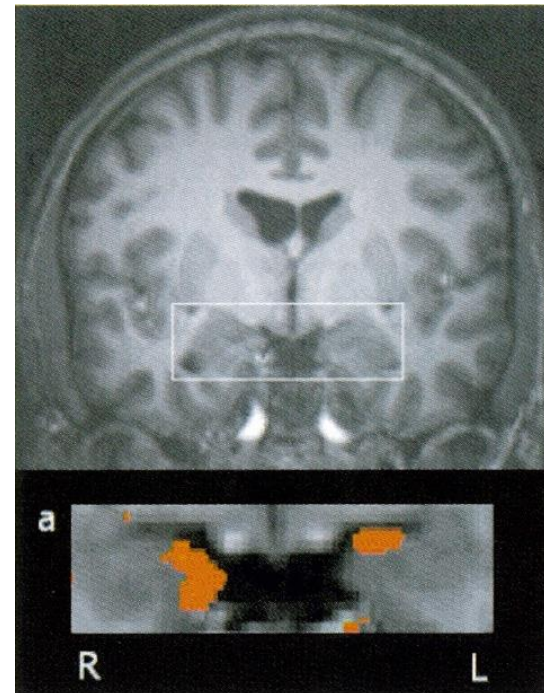


Speculation and Surprise

- Surprise depends on expectations
- In a speculative bubble, expectations are high
- So, sudden departures are especially surprising and salient
 - $\alpha\beta$ is high
- So fear learning is fast...
- Is it contagious?

Observational Fear Conditioning*

- Shown earlier : Fear-Conditioned human amygdala fMRI
- US: Shock cuff
- UR: Amygdala activation
- CS: Blue Light (neutral)
- CS-US Pairing Trials
 - Light...Shock
 - Light...Shock
 - Light...Shock
 - Light alone→

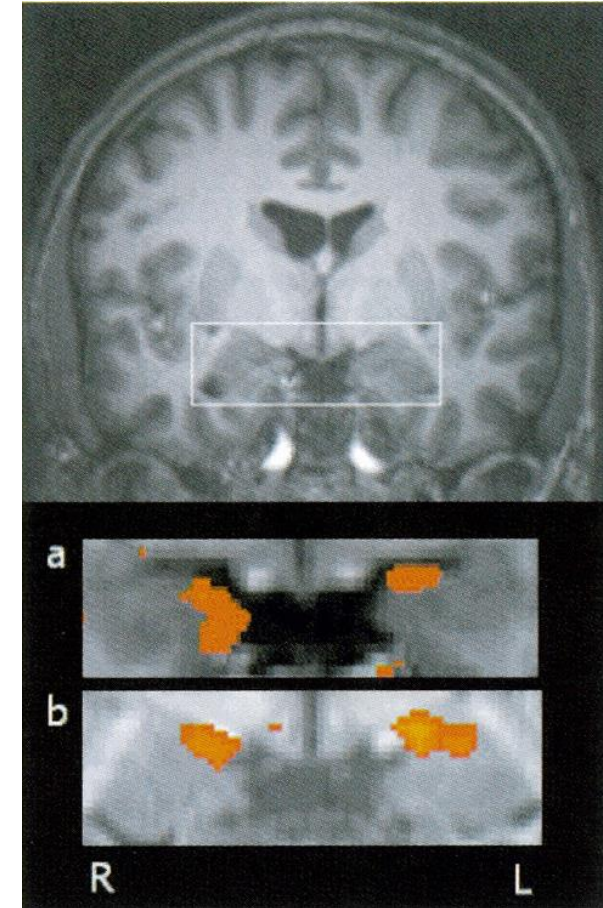


*Olsson, A., Nearing, K. I., & Phelps, E. A. (2007). Learning fears by observing others: the neural systems of social fear transmission. *Social cognitive and affective neuroscience*, 2(1), 3–11.

Is Fear Contagious?

- Top Panel (a), fMRI of subject above
- True Subject: Bottom Panel (b), fMRI of *observer*.
- Watches the blue-shock pairings
 - Then is shown blue light alone...
 - Same fMRI as if conditioned!
- Advantage clear
 - I learn to fear the fire by watching you get burned
 - Downside is also clear: rapid nonconscious transmission of baseless fear.

Double -edged



Perils of Fitness

- “Survival circuits” (LeDoux 2012) conserved across vertebrate evolution.
- Epstein (2013) “Pleistocene man never encountered a BMW, but *we* freeze when a car whips around the corner at us, just as *he* froze when huge animals charged suddenly from the tall brush. *We are harnessing the same innate fear-acquisition capacity—the same innate neurochemical computing architecture.* Miraculously, synaptic plasticity permits us to adapt the evolved machinery to encode novel threats.”
- Invaluable but very dangerous...double-edged

Surprise + Salience → Strong Conditioning

CS	US	UR/CR
Light	Shock	Fear
Vietnamese Face	Ambush	My Lai
Arab Face	9/11	Koran as ISIS Field Manual
Japanese Face	Pearl Harbor	Internment

Surprise + Salience → Strong Conditioning

CS	US	UR/CR
Light	Shock	Fear
Doctor	Tuskegee	Distrust
MMR Vaccine	Autism	Vaccine refusal
Financial asset	Sudden devaluation	Panic!

Also Over-General and Persistent

- *Should* stay afraid of hippos.
- Affect can remain above the threshold long after actual stimulus has stopped.
- Stimulus stopped at t . Extinction may be far off. Extreme case is PTSD.
- Not Symmetrical

Full Affective Trajectory (vigilance and complacency)

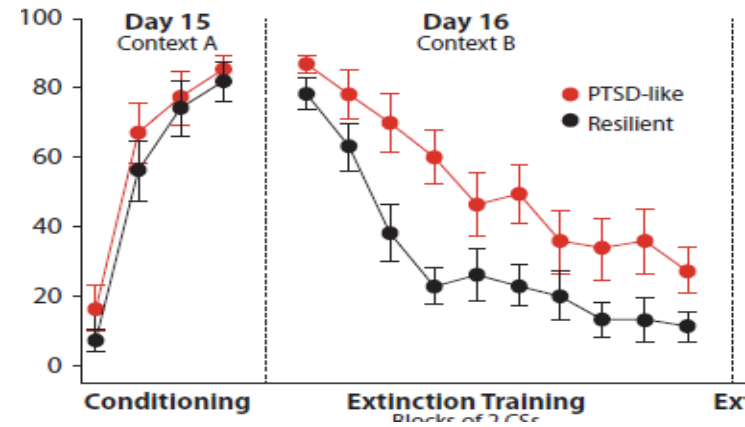
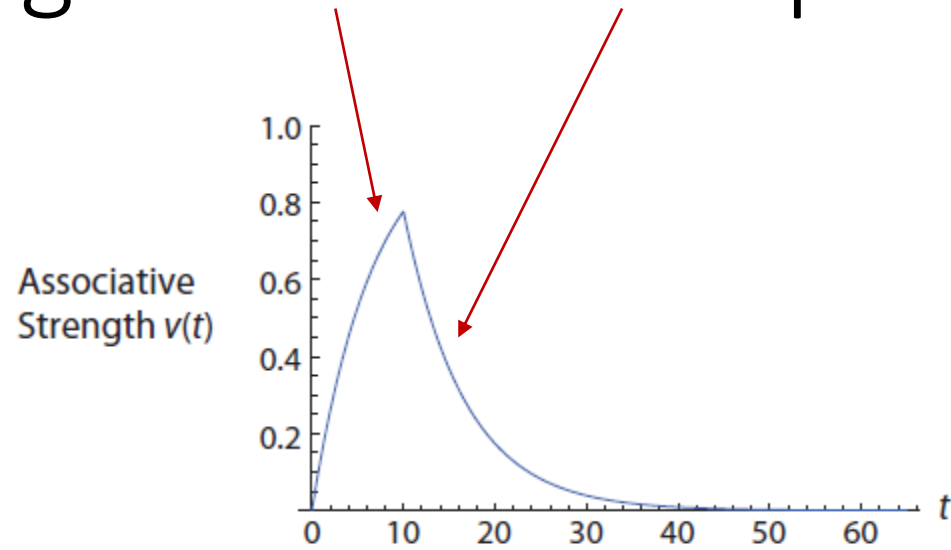


FIGURE 8. Acquisition and Extinction

Rats, predatory threat

With t^* the time at which trials cease, the full solution is then

$$v(t) = \lambda(H(t^* - t)(1 - e^{-\alpha\beta t}) + (1 - e^{-\alpha\beta t^*})H(t - t^*)e^{-\alpha\beta(t - t^*)})$$

We do not fear *what* the rat fears, but we fear *how* the rat fears.

Ingredient 1: Emotion

- Introduce a generalized version of the classic (1972) Rescorla-Wagner model and emotional contagion through weights (endogenous functions of affect in book).

Reason may be “a slave to the passions,” a la Hume but once in a great while, it happens...however badly!

- Typically we have incomplete and imperfect information
- Make systematically erroneous appraisals of it.
- Robustly documented errors:
 - Framing effects (medical decisions)
 - Endowment effects (loss aversion)
 - Representativeness heuristic
 - Local sample represents population
 - Base rate neglect
 - Confuse $P(+ | \text{sick})$ with $P(\text{sick} | +)$
 - Anchoring on what you hear first
 - $2345678 < 8765432$
- *Agent_Zero* (local relative frequentist) exhibits several.

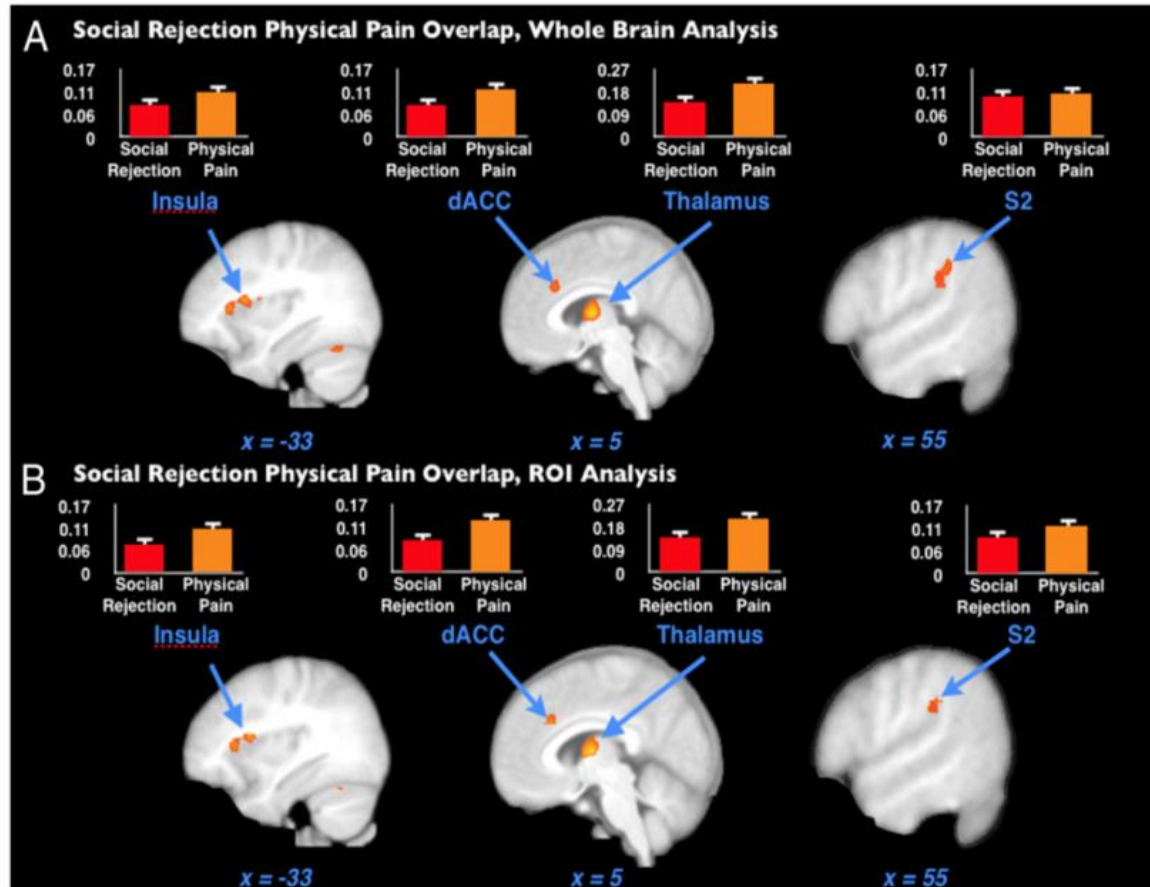
To Make Matters Worse...

- Agents driven by strong (unconscious) emotions (like fear), doing bad statistics on incomplete and biased data, also *influence* one another.
- Conformist pressures can then produce widespread convergence on counter-productive behavior.
- Conformity effects are documented in many spheres (since Asch 1958).
- Again, a neural basis?

Yes: Nonconformity Hurts!

- Kross et al (*PNAS* 2011) “...when rejection is powerfully elicited...areas that support the sensory components of *physical pain* (secondary somatosensory cortex; dorsal posterior insula) become active.”
- Illustrated in fMRIs below.

Neural Drivers of Conformity



Neural overlap between social rejection and physical pain.

Bar graph: no statistically significant difference between (β s of) rejection and physical pain. Positive predictive value = 88%.

Source: Kross, E., Berman, M. G., Mischel, W., Smith, E. E., & Wager, T. D. (2011). Social rejection shares somatosensory representations with physical pain. *Proceedings of the National Academy of Sciences of the United States of America*, 108(15), 6270–6275.

Conform Because Rejection Hurts.

- As they write, “These results give new meaning to the idea that rejection ‘hurts’...rejection and physical pain are similar not only in that they are distressing—they share a common somatosensory representation as well.”
- We give others weight...so

Ingredient 3: Network Weights

- Agents experience a weighted sum of the affective and deliberative states of others
- As discussed, weights are actually endogenous in model—strength-scaled affective homophily *generates* networks...more on this in the Master Class.

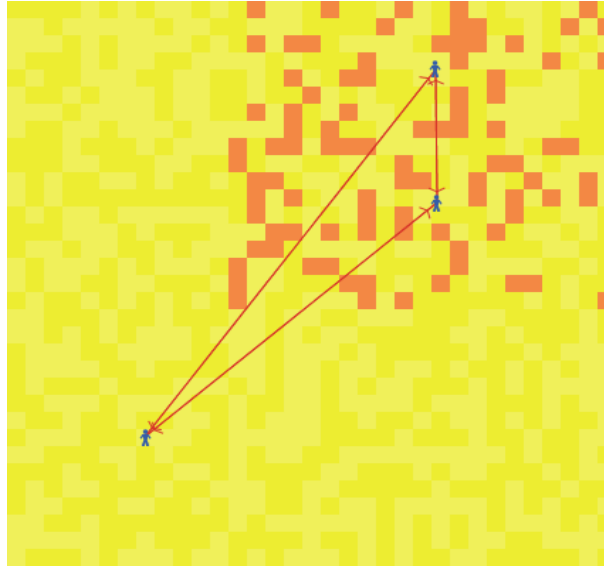
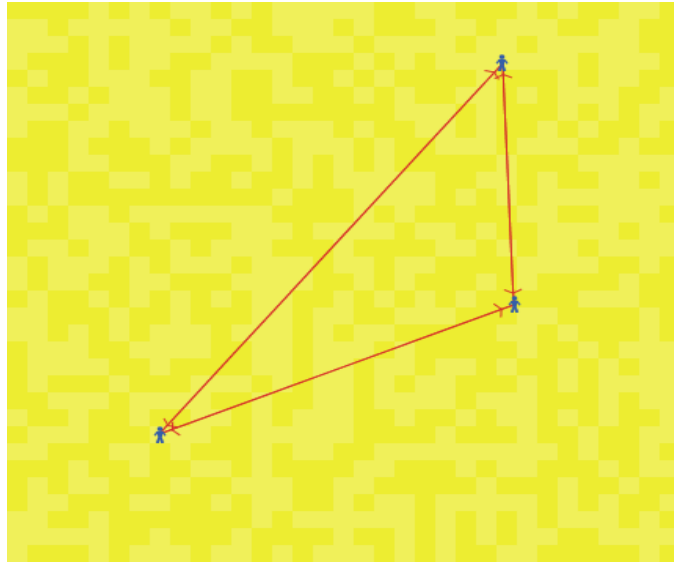
Given these components...

- Logic of the Model:
 - Disposition
 - Threshold
 - Action
 - This typically alters the stimulus pattern

Agent-Based Model Runs : Computational Parables

All Code for ODEs and for the ABM, all parameter values, all initial conditions and random seeds are at the Princeton Press *Agent_Zero* site. Replicable.

Landscape and Trials: Agent_0 Fixed and Mobile Rovers



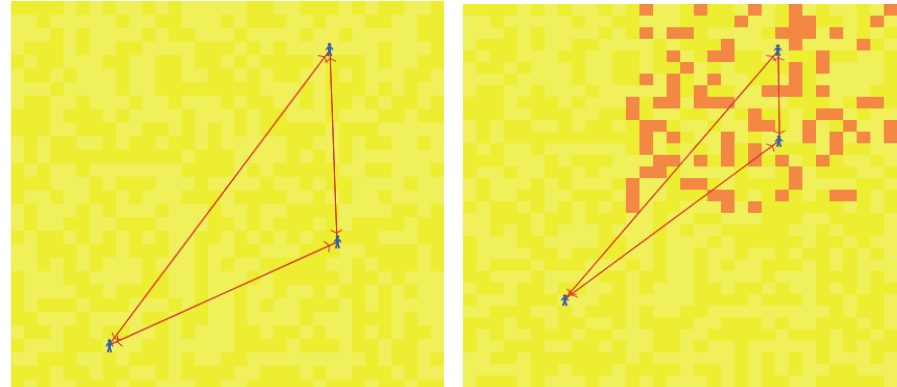
Agents directly condition on orange trials and compute RF w/in vision.
Then a weighted sum over network. If $D > \tau$, destroy all sites w/in
damage radius

Parable 1: Slaughter of Innocents

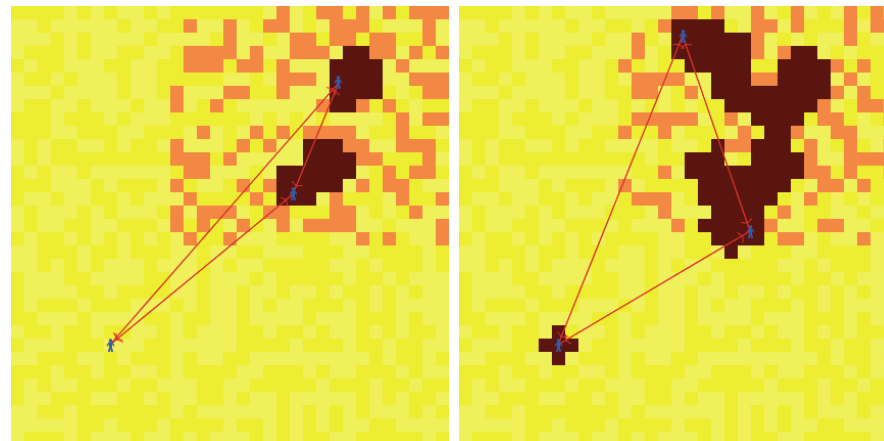
Agent 0 fixed, zero direct stimulus

Mobile rovers transmit retaliatory disposition

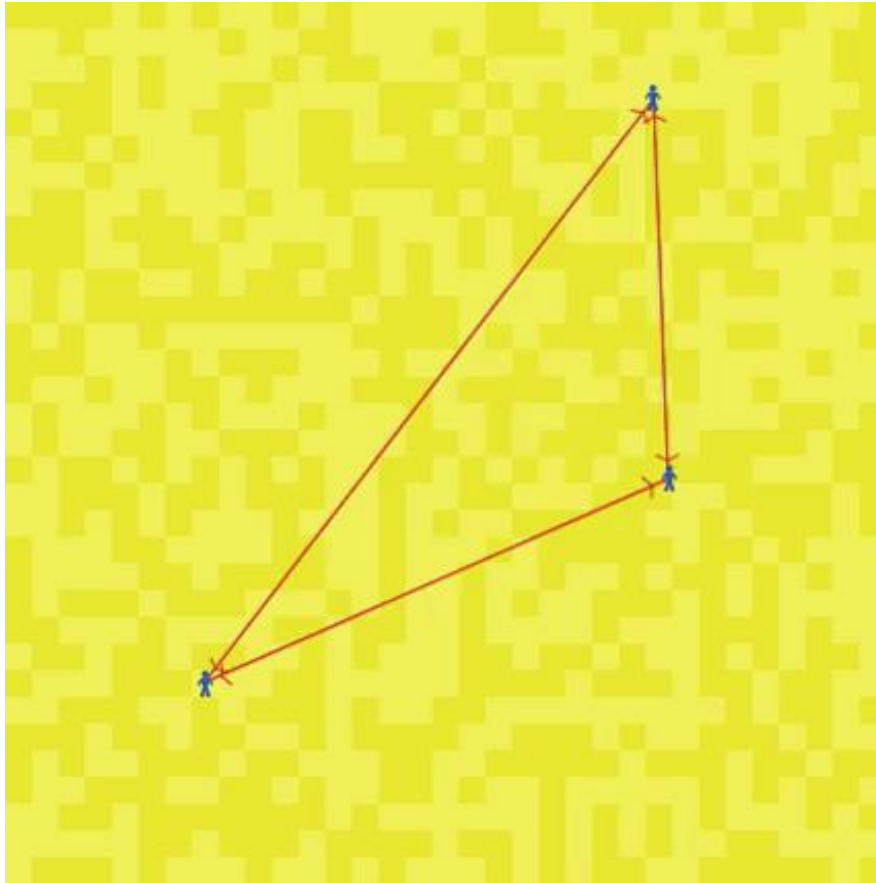
Vision Von Neumann.....Agent 0 massacres village



Animation 3.3. Activation by Dispositional Network Effect:



Parable 1: Agent_Zero Joins Without Direct Stimulus



$V=P=0$, since no stimulus within sensory radius

Solo disposition = 0

Eye candy is one sample path. Turn off and build statistical portrait.

La Condition Humaine

- Why?

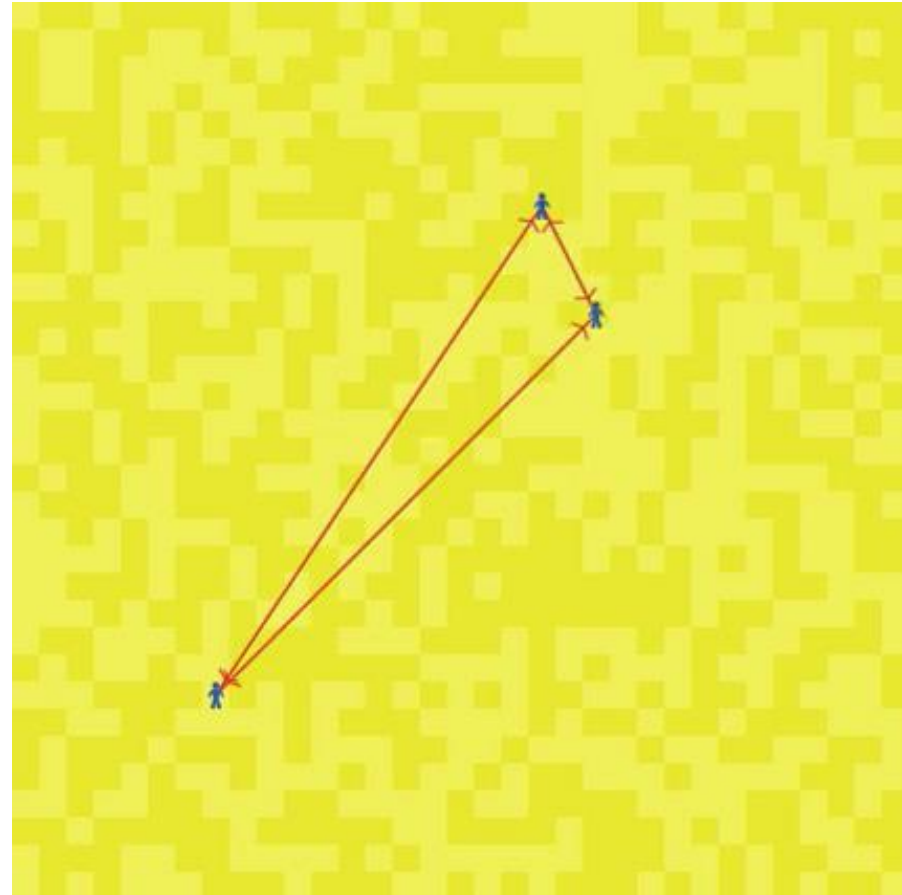
$$D_i^{Tot}(t) > \tau > D_i^{Solo}(t)$$

- You take action in group (since $D_i^{Tot}(t) > \tau$) that you would not take alone (since $\tau > D_i^{Solo}(t)$).
- Indeed, you may be the only agent with this ordering. In that case:
- *Despite being negatively disposed* you act first!*

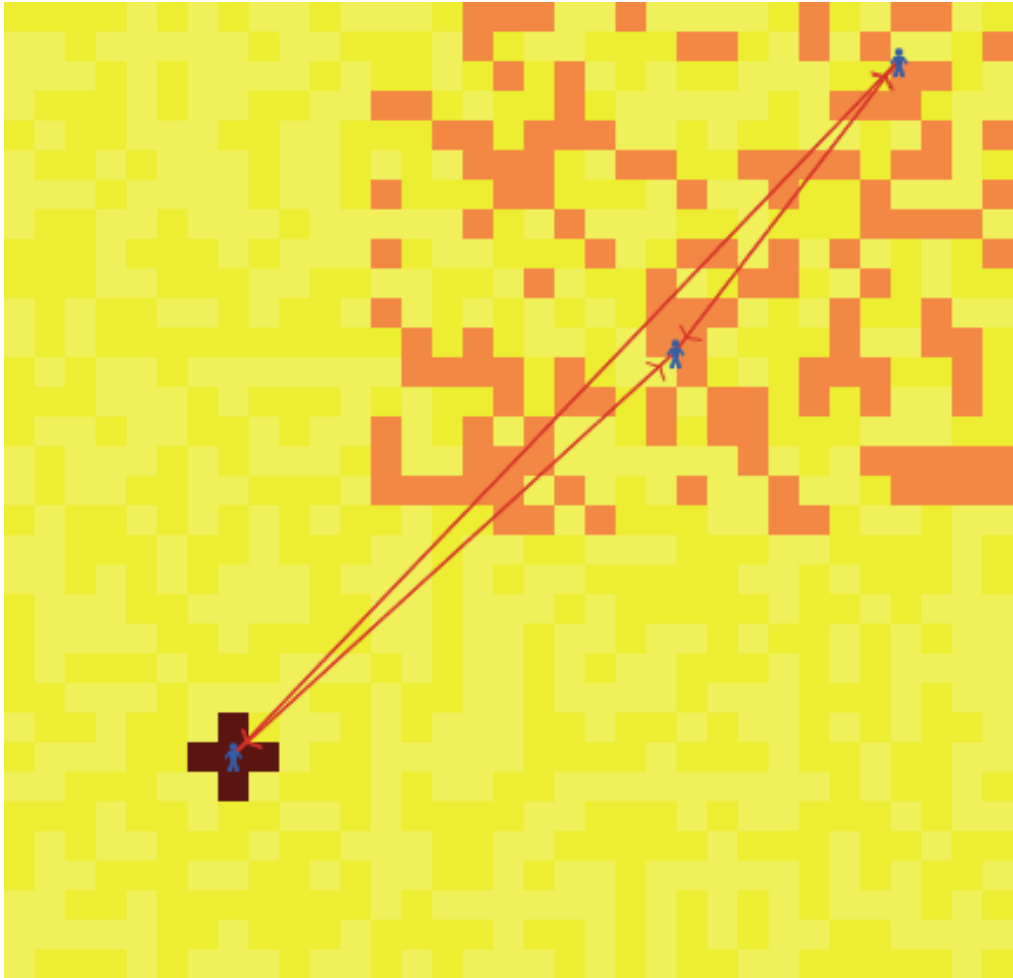
* $D_i^{Solo}(t) - \tau < 0$

Parable 2: Agent Zero Initiates

- Again, **no** direct stimulus
- He goes first!
- Not imitation of behavior



Core Parable: Agent_Zero Goes First Without Stimulus



Leadership or Susceptibility?

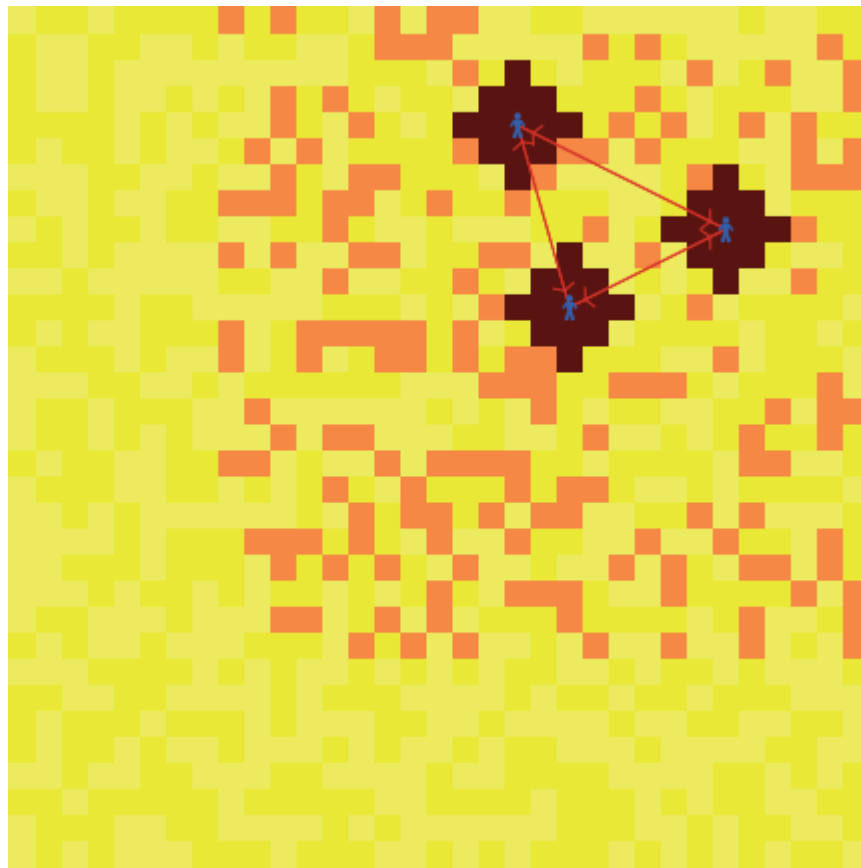
- Not behavioral imitation.
 - If 1st, nobody to imitate
- Leader, or just most susceptible to D-contagion?
- Tolstoy's answer: 'A king is history's slave, performing for the swarm life.' (*War and Peace*, 1896)

Unsettling Picture

“The overall picture of Homo sapiens reflected in these interpretations of *Agent_Zero* is unsettling: Here we have a creature evolved (that is, selected) for high susceptibility to unconscious fear conditioning. Fear (conscious or otherwise) can be acquired rapidly through direct exposure or indirectly, through fearful others. This primal emotion is moderated by a more recently evolved deliberative module, which, at best, operates suboptimally on incomplete data, and whose risk appraisals are normally biased further by affect itself. Both affective and cognitive modules, moreover, are powerfully influenced by the dispositions of similar—equally limited and unconsciously driven—agents. Is it any wonder that collectivities of interacting agents of this type—the *Agent_Zero* type—can exhibit mass violence, dysfunctional health behaviors, and financial panic?” (Epstein, 2013)

Fight vs. Flight

- Fight

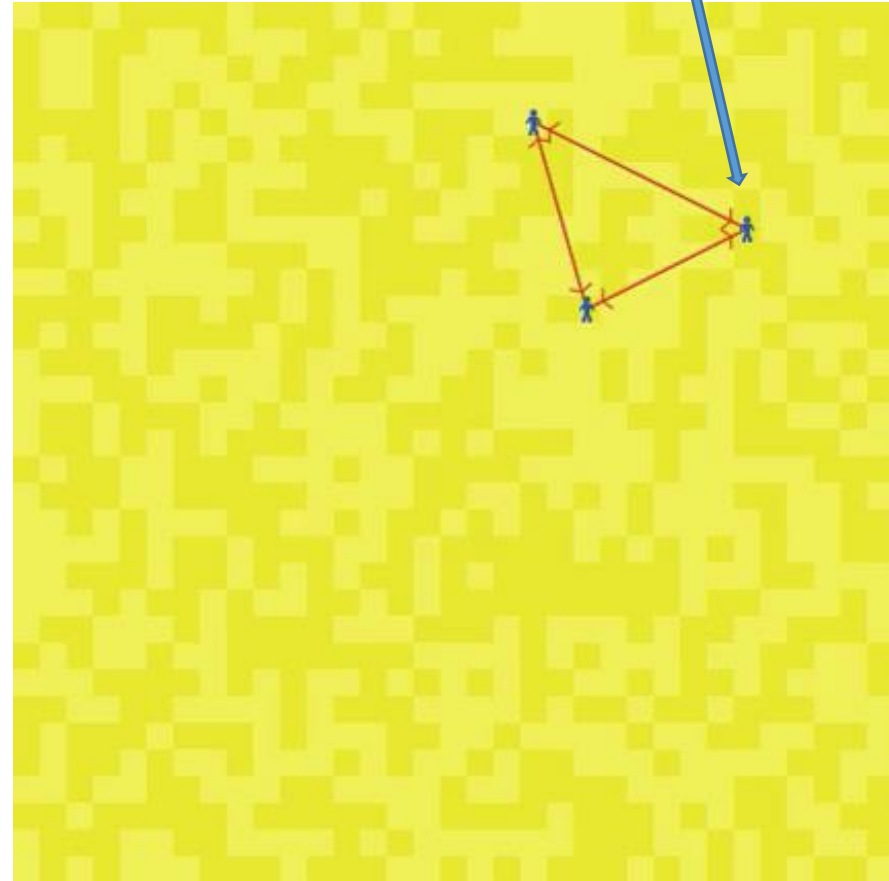


Flight

- Katrina Evacuees
- Syrian Refugees
- Capital/Portfolio Flight

- Recalcitrant agents “dragged out” by others.

Would not flee her portfolio alone



Taking Animal Spirits Seriously

- Make the action the purchase of some commodity (or quantity) at prevailing prices (*Agent_Zero* a price-taker).
- Make the Action threshold (τ) price-dependent in an orthodox (convex) way

$$\tau'(p) > 0, \tau''(p) < 0, \tau(0) = \tau_0$$

- The model generates observed seasonal demand cycles (Epstein 2014)
- Take *Animal Spirits* (Keynes, Akerlof) seriously.

Main Thought...

- “...my earlier remarks about using the *Agent_Zero* framework to study financial contagions, the collapse of spatially explicit housing markets, or other cascading dynamics is far from idle. Given relevant data, the replication of historical examples—economic and otherwise—could profitably be attempted.” Epstein (2013, p. 176)

Promising line of Agent_Zero Economics

- One of Alan Kirman's mentees.
- Americ Vye, "Information Selection Efficiency in Networks: A Neurocognitive-Founded Agent-Based Model," in Chakrabarti, et al, Eds. *Network Theory and Agent-Based Modeling in Economics and Finance* (Springer, 2019)

In all of this, Networks are Implicated

- How do network weights change?
- Why do networks happen?

Endogenous Weight Change by Affective Homophily (so weights are not parameters)

- Affective homophily. Affects changing. So try: $|v_i(t) - v_j(t)|$
- Problem: equals zero when identical; want 1.0 when equal.
- OK, so as homophily, use: $1 - |v_i(t) - v_j(t)|$
- Problematic as a weight: nudniks ($v=0$) same strength as crusaders ($v=1$). So, scale by total strength

$$\omega_{ji}(t) = [v_i(t) + v_j(t)](1 - |v_i(t) - v_j(t)|)$$

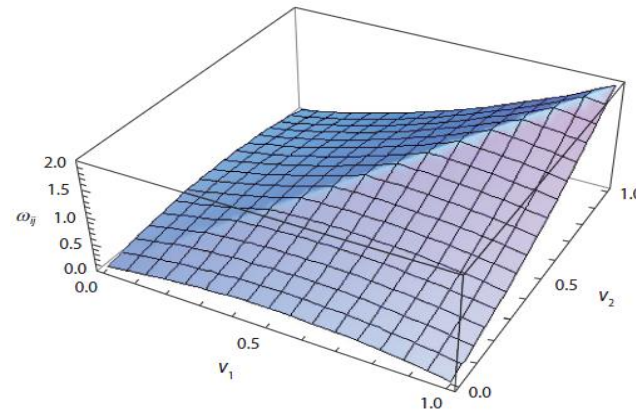
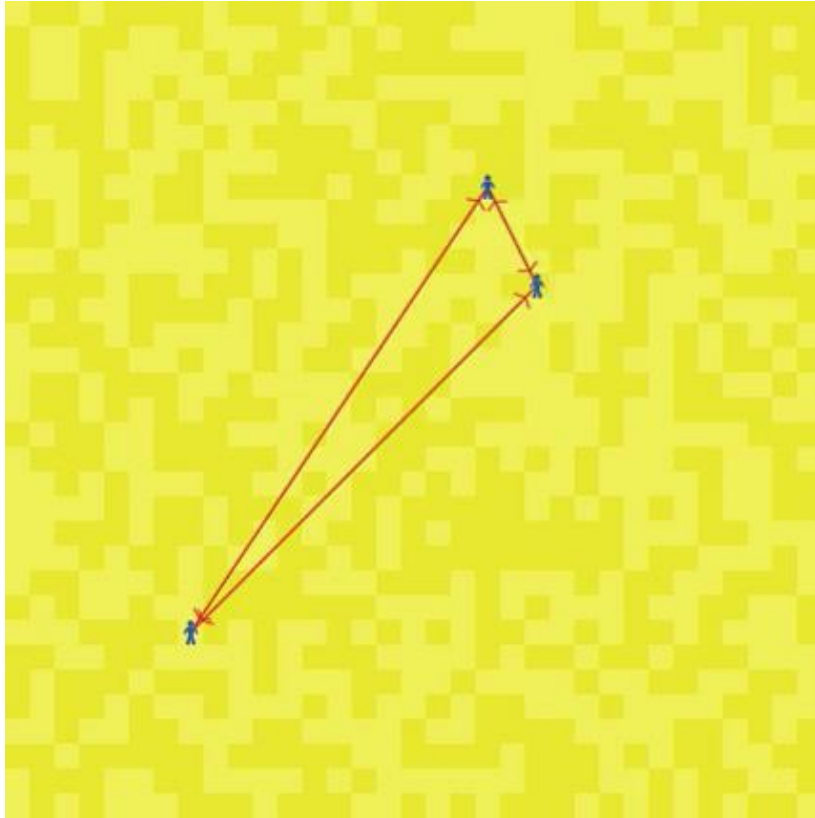


FIGURE 63. Weight Surface

Endogenous Weights:



- Affective homophily strengthens connection
- And this can matter immensely...

Grow The Arab Spring

Case 1: No Communication

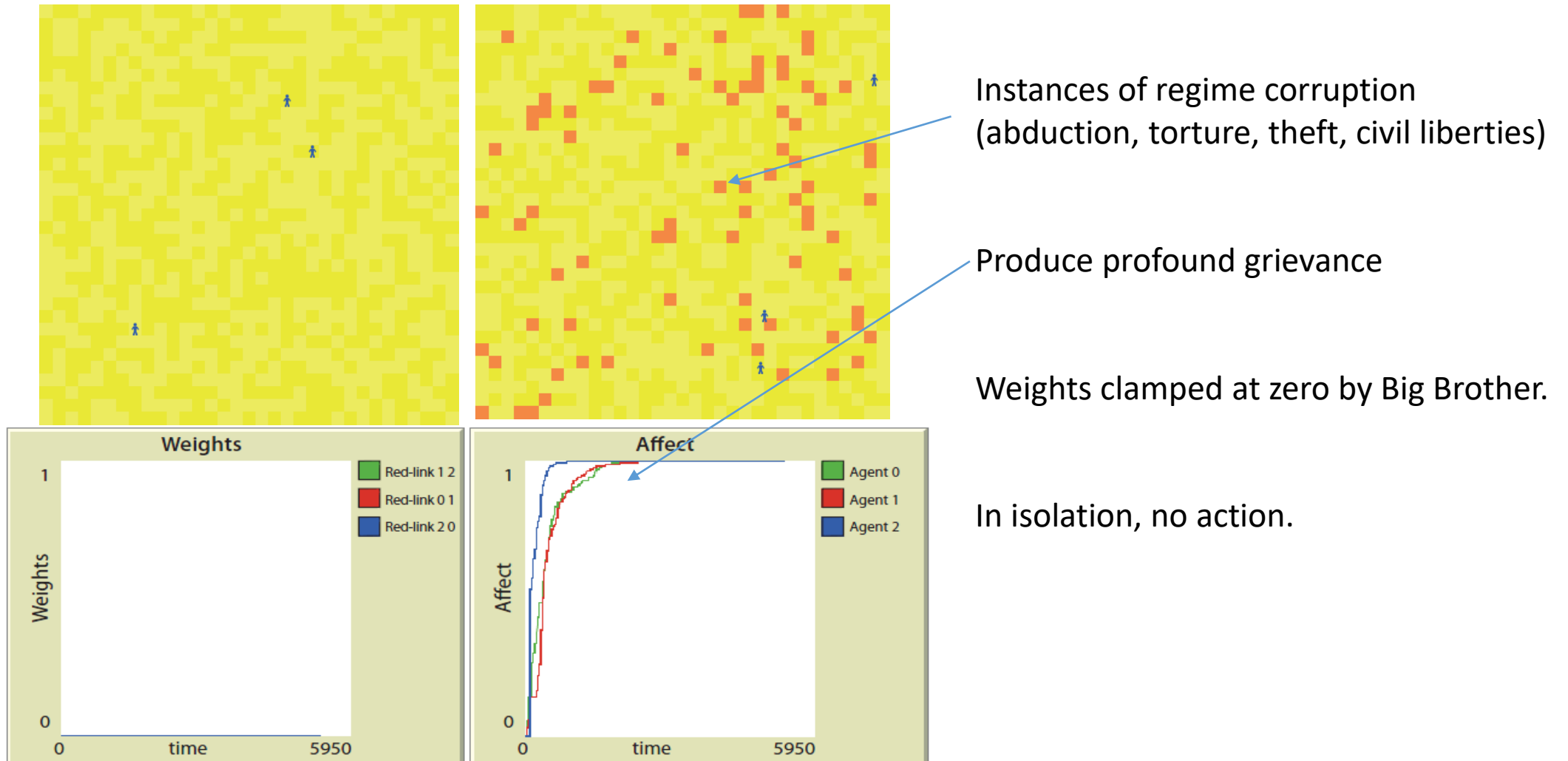
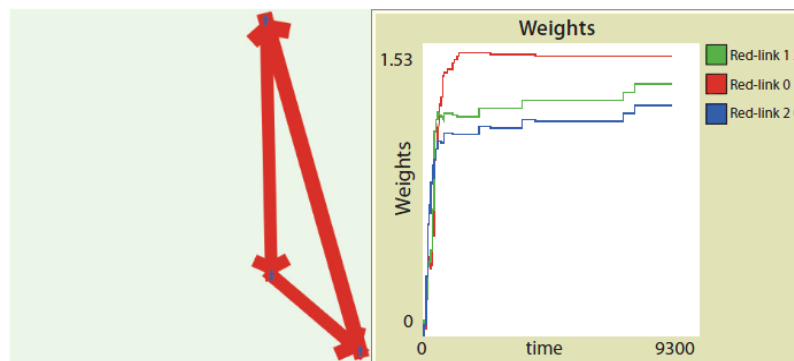
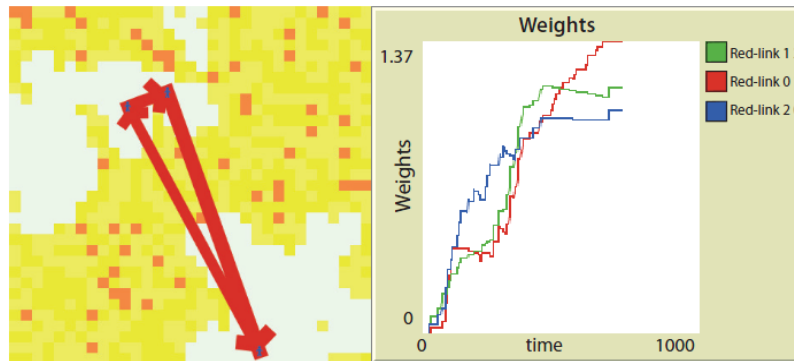
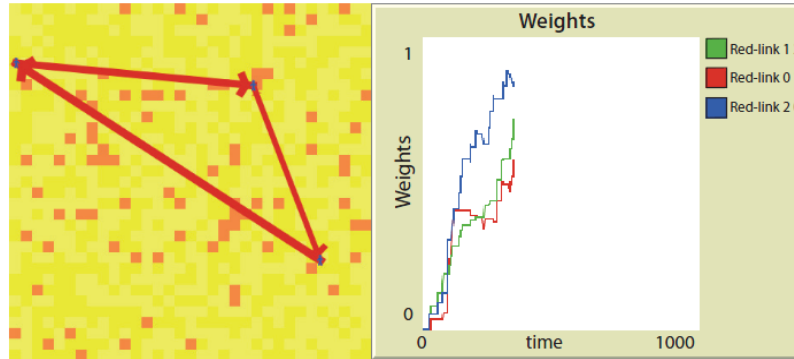


FIGURE 73. Weights and Affect with No Social Media

Arab Spring (Jasmine Revolutions)

Case 2: Communication → Dispositional Amplification → Overthrow



Revolt of the Swarm

- Leaderless Revolutions
 - No Mao, Lenin

- Similarly in Juries

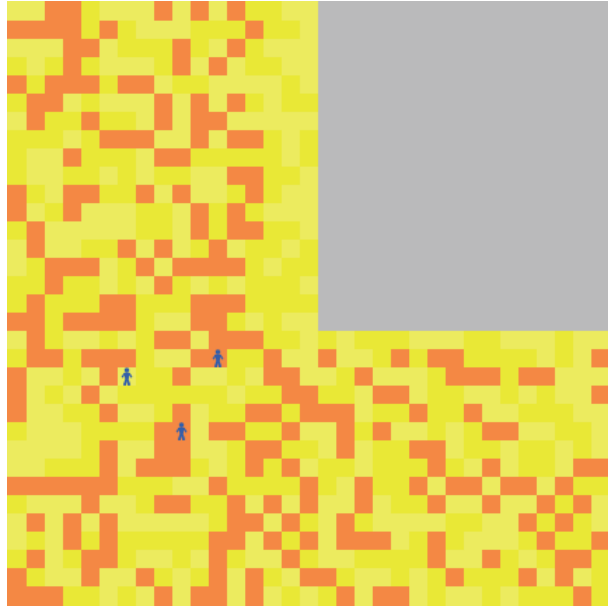
Jury Dynamics:

12 Angry Agent_Zeros

- **Pre-Trial:** General landscape of stimuli about OJ's guilt. Initial dispositions to convict are formed. Jurors strangers. All weights off.
- **Trial:** Competing stimuli (Prosecution and Defense). Dispositions are updated. Jurors do not communicate. Weights still off.
- **Sequestration:** Now homophily dynamics and network effects operate strongly.
- Agents convict in group when they would acquit alone:

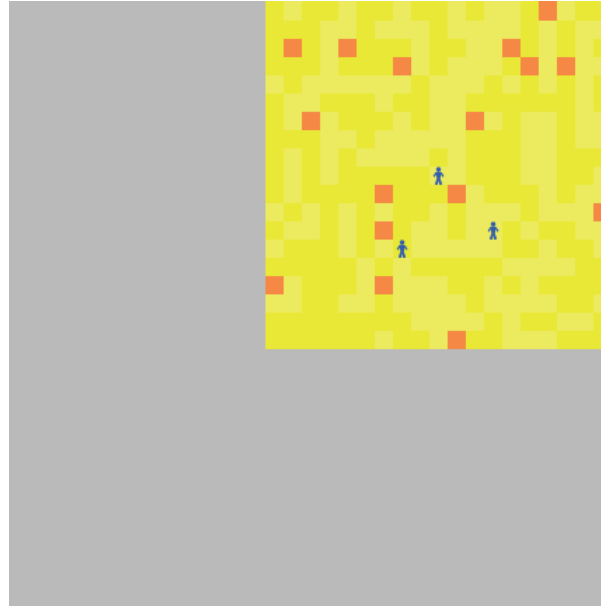
Three-Phased Trial

Pre-trial



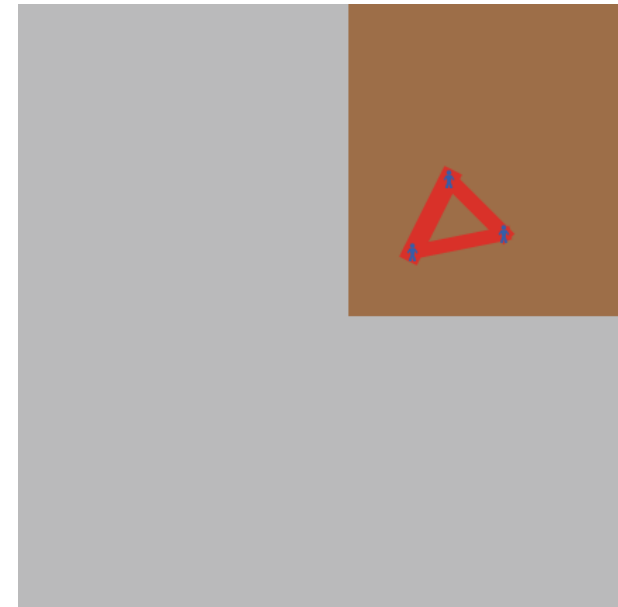
Pre-trial: $S_1 > 0$, $\omega = 0$

Courtroom



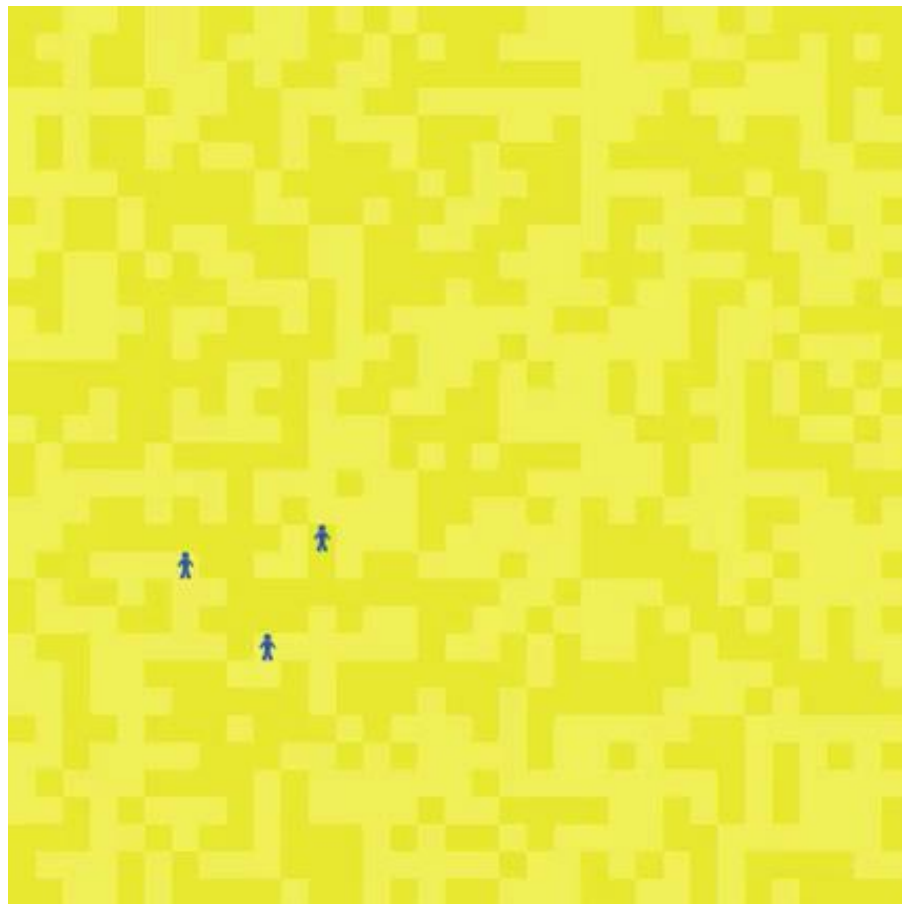
Courtroom: $S_2 > 0$, $\omega = 0$

Jury Chamber

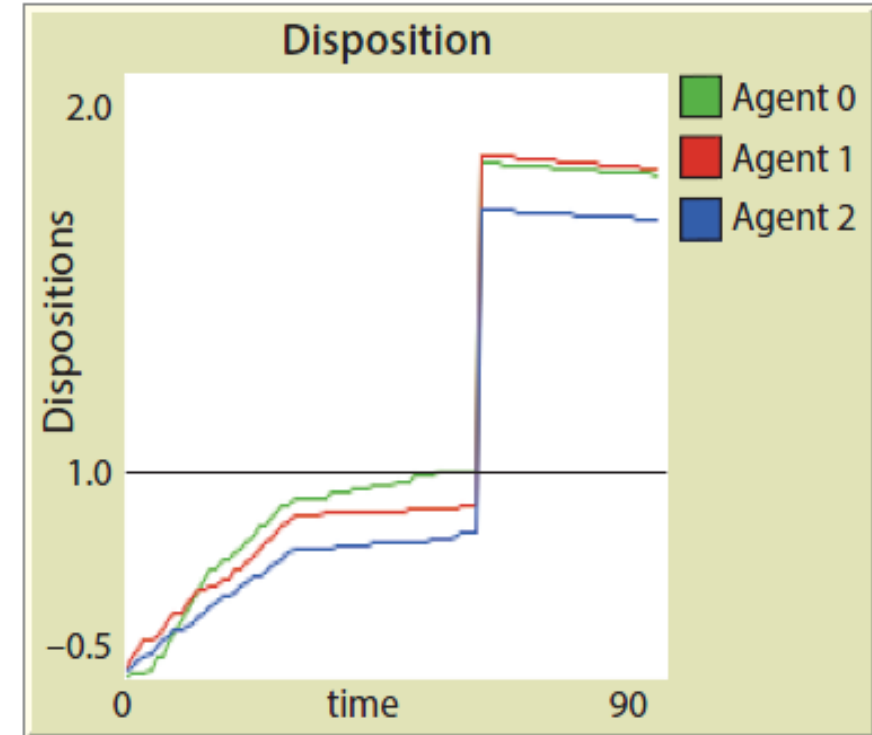
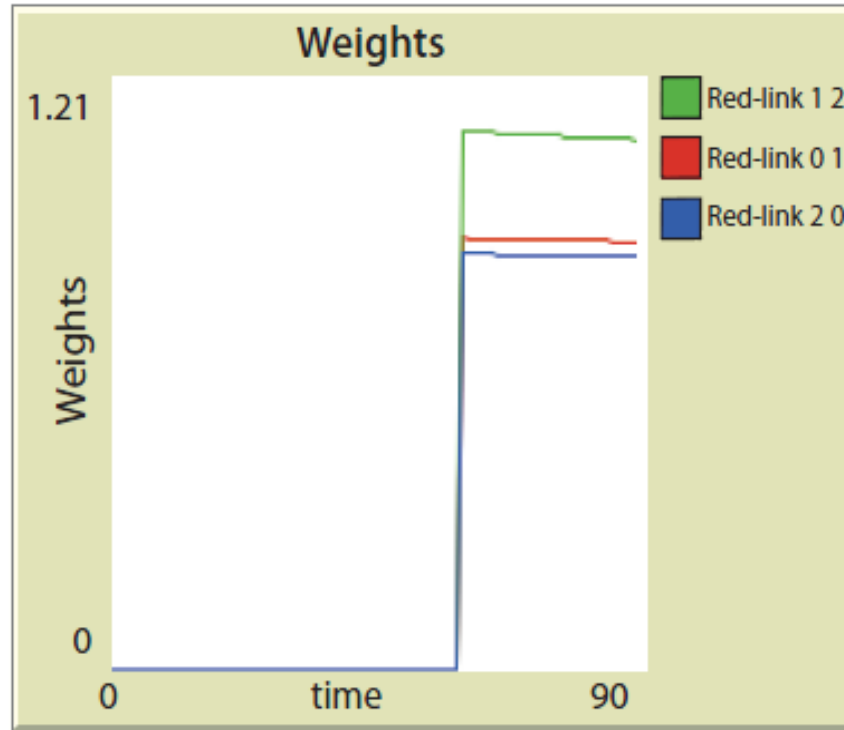


Jury Phase: $S_3 = 0$, $\omega > 0$

Jury Trial



Weights Jump in Jury Chamber. Drive Dispositions to Convict



Universal Self-Betrayal

$$\forall i, D_i^{total} > \tau > D_i^{solo}$$

No jurors would have convicted before the jury phase, but they are unanimous in rendering a guilty verdict, having interacted directly.

Why Do Networks Happen? Come to Master Class...

- “Network structure” : links exist or not: $\{0,1\}$
- We have continuous weight dynamics but want to study structure.
- How to filter the continuous affinity dynamic onto binary structure of nodes and edges?
- Introduce a link threshold τ_L
- Link exists if and when $\omega_{ji}(t)$ exceeds τ_L

Mathematically

$$L_{ij}(t) = \begin{cases} 1 & \text{if } \omega_{ij}(t) > \tau_L \\ 0 & \text{otherwise} \end{cases}.$$

using the Heaviside unit step function

$$L_{ij}(t) = H(\omega_{ij} - \tau_L).$$

Different Thresholds Yield Different Structure History

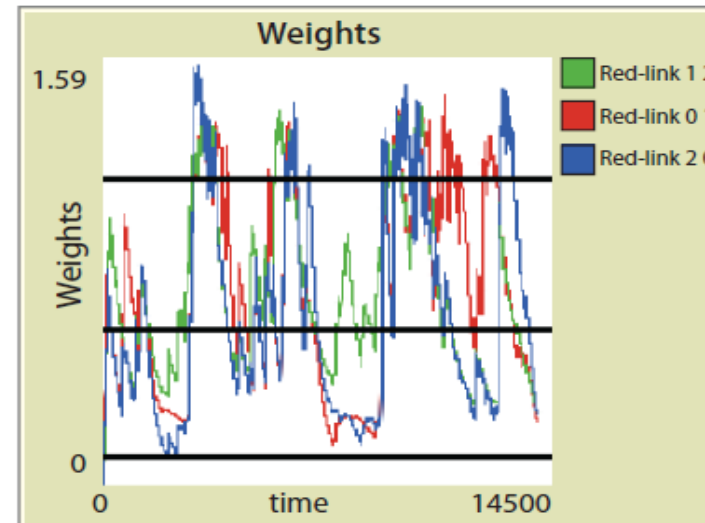
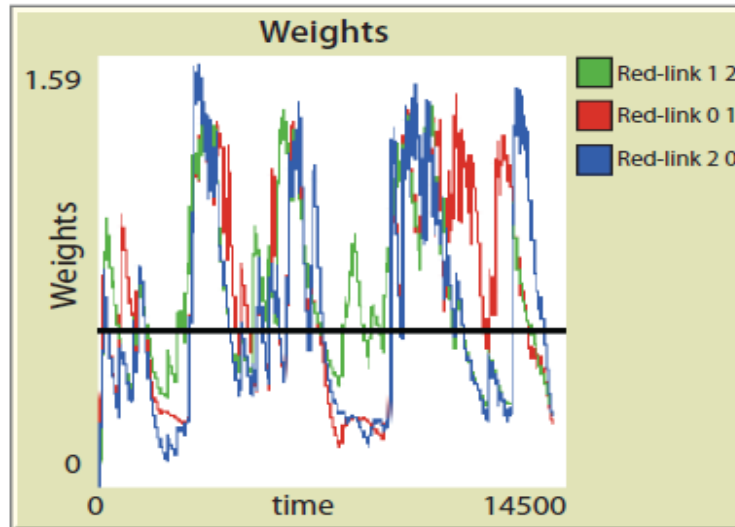


FIGURE 87. Episodes of Connection

Structure as Function of Threshold

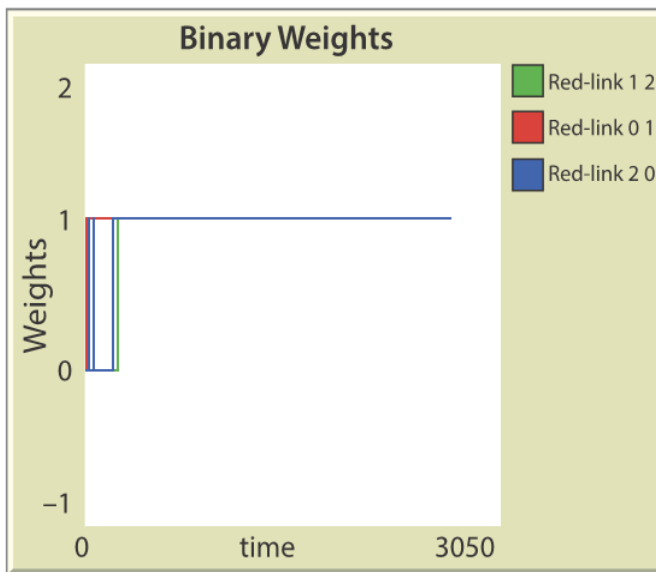


FIGURE 94. Threshold 0.25

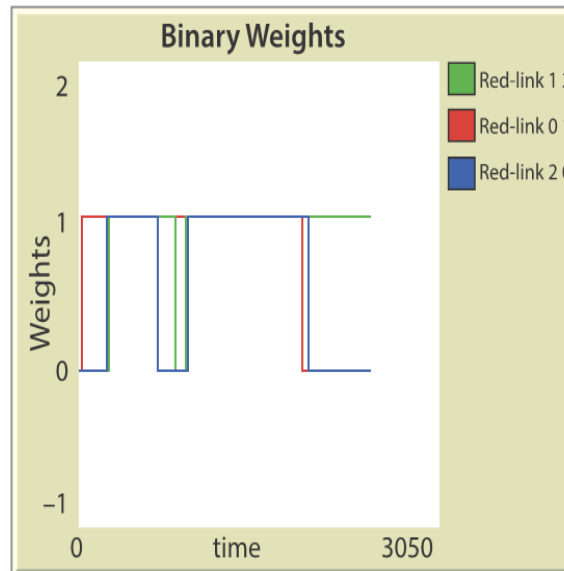


FIGURE 95. Threshold 0.5

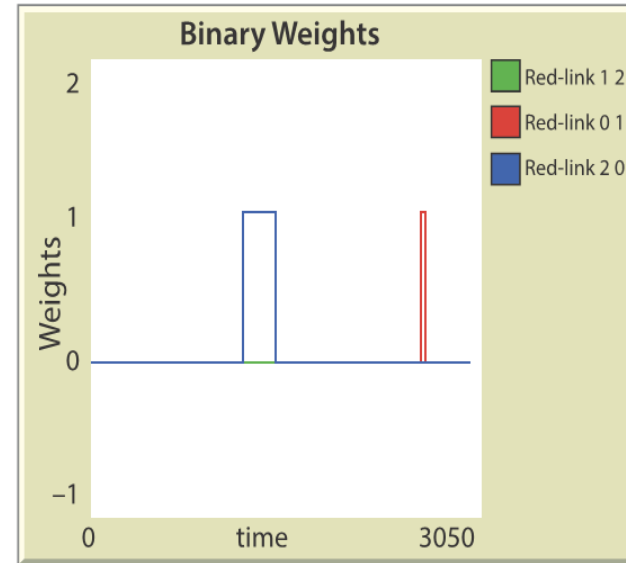
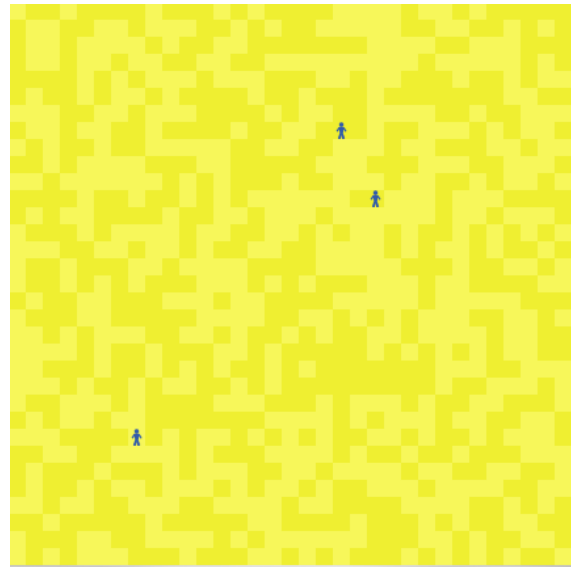


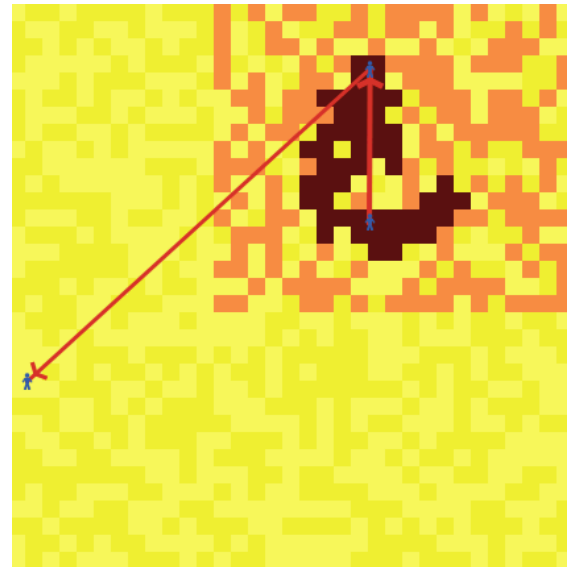
FIGURE 96. Threshold 1.0

For the same affinity dynamics, different thresholds produce different structure dynamics

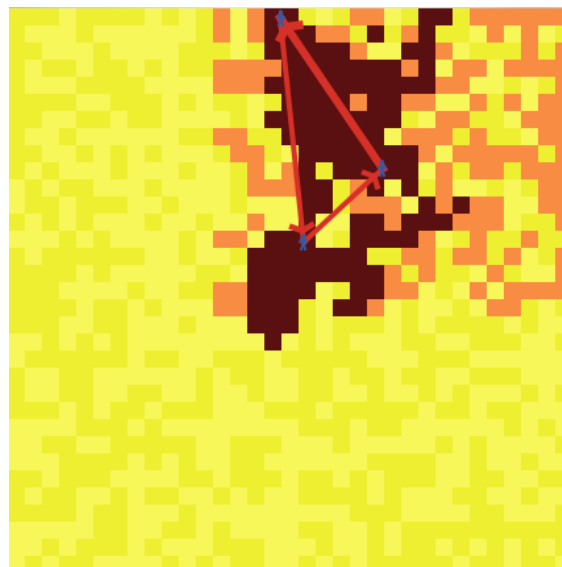
Link Formation and Breakage: Dynamics of Structure Proper



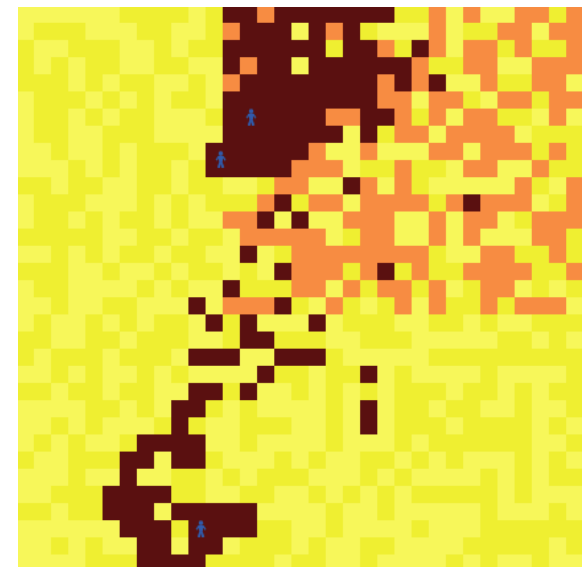
None



Partial



Full



None

Part III: Extensions and Foundational issues

Epstein, JM and Chelen J , “Advancing Agent Zero” in Kirman A and Wilson DS, eds. *Complexity and Evolution: Toward a New Synthesis for Economics* (MIT Press, 2016)

Extensions

- Scale-Up to large numbers
- Permit arbitrary network topologies (Master Class on How)
- The most arresting Parable, to me, is the first actor:
- An agent that has no aversive stimulus and would not act alone leads the lynch mob, by dispositional contagion.
- How robust is that?
- For arbitrary numbers of northerners (with stimulus) and southerners (without) and arbitrary network topologies, it is mathematically formidable.
- Preliminary computational experiments very interesting.

setup

go

Agents

attack_rate 401

extinction_rate 0.71

spatial_sample_radius 3

action_radius 1

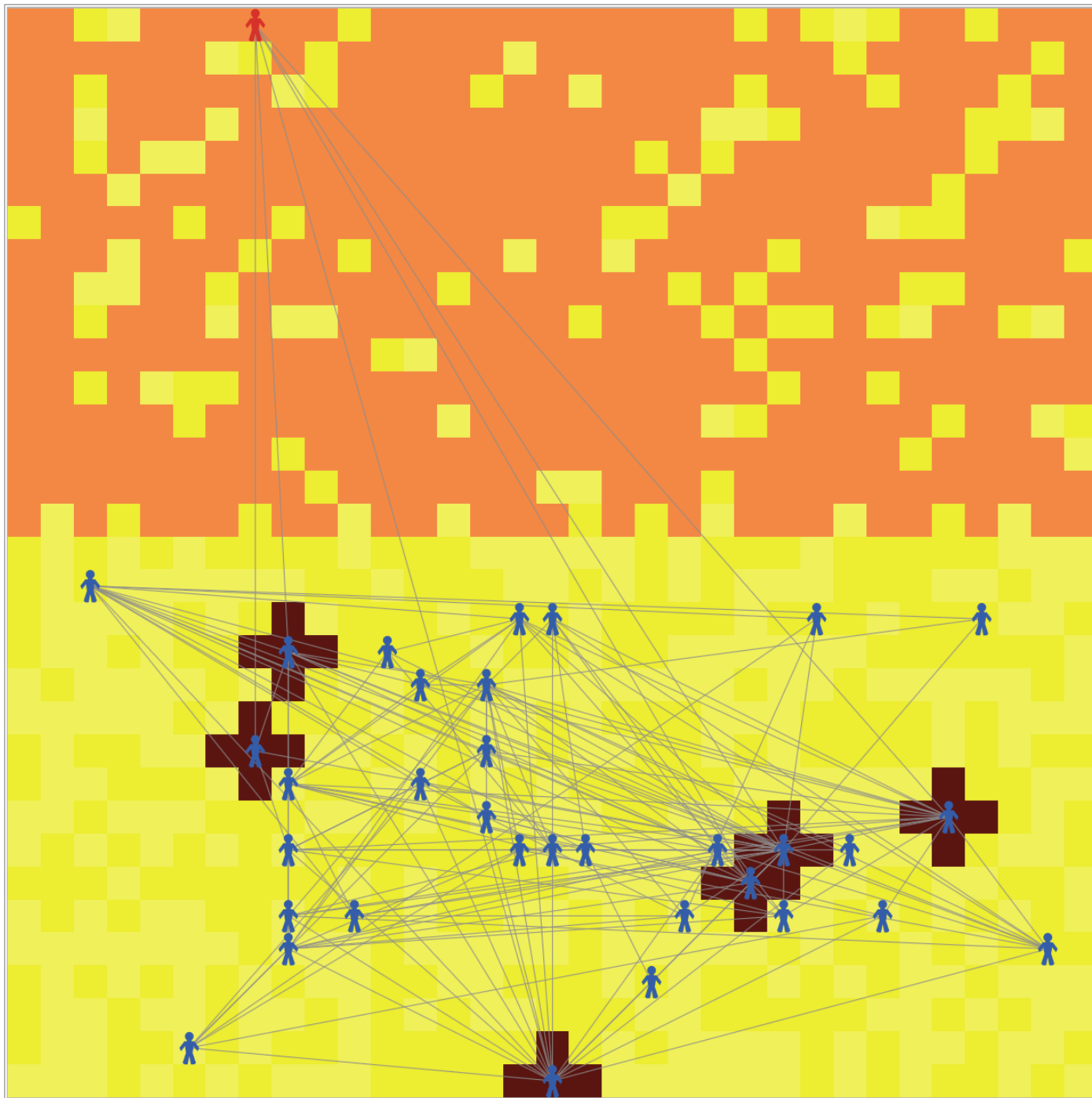
memory_length 8

Network

number-of-nodes 66

degree 8

count turtles
34



Explorations

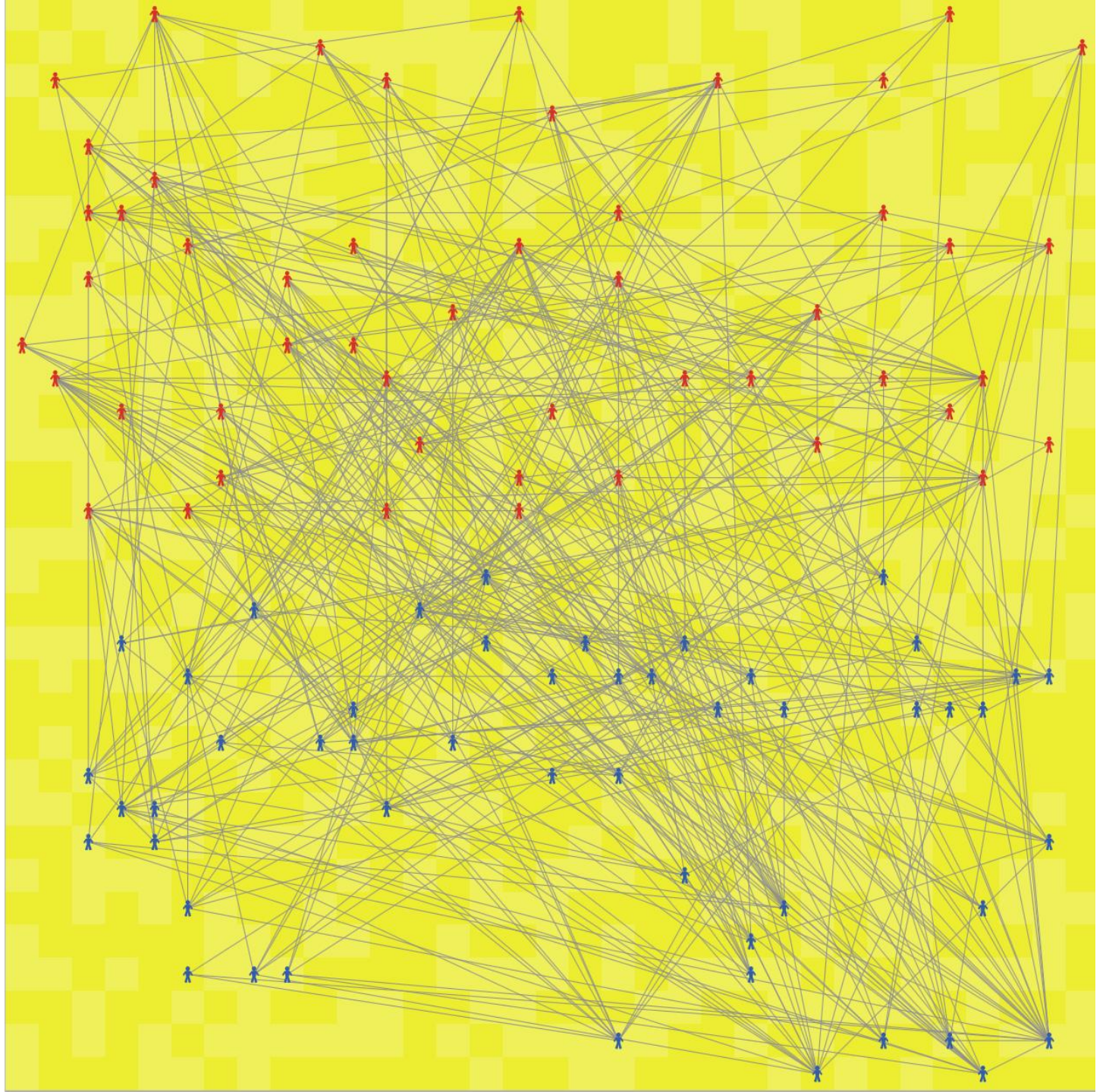
Can scale up and stipulate fixed network structures and explore dynamics computationally

Exponential degree distribution ($\lambda=5$)



Turn off all the movies, assume distributions and prove some theorems on core phenomena:

- [1] waiting time to first actor,
- [2] probability of universal self betrayal.



setup go

model-seed-option
Random seed

num-people 100
num-northerners 2

attack_rate (max=1000)
60

vision 3
memory_length 8

extinction_rate (max = 1.0)
0.7

action_radius 1

northerner-thr
0.5

southerner-thr
0.5

update-weight
no update

On movement?
Off

social-connection
random exponential

s-to-s-init-link-weight
0.5

s-to-n-init-link-weight
0.1

n-to-n-init-link-weight
0.1

n-to-s-init-link-weight
0.8

s-to-s-num-links-or-mean-exp-num-links
4

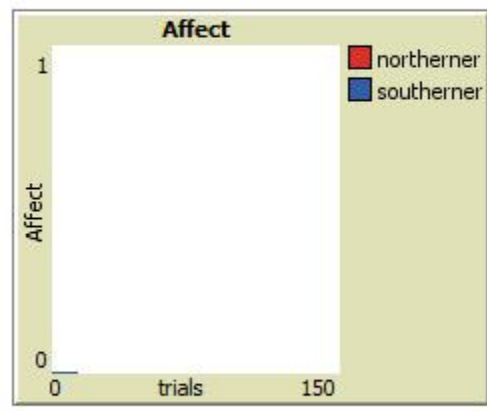
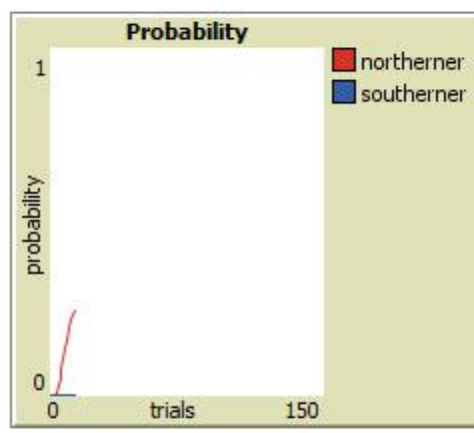
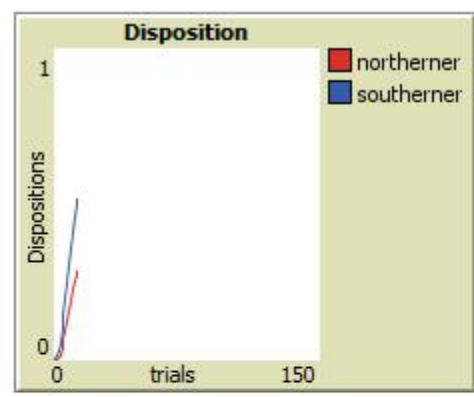
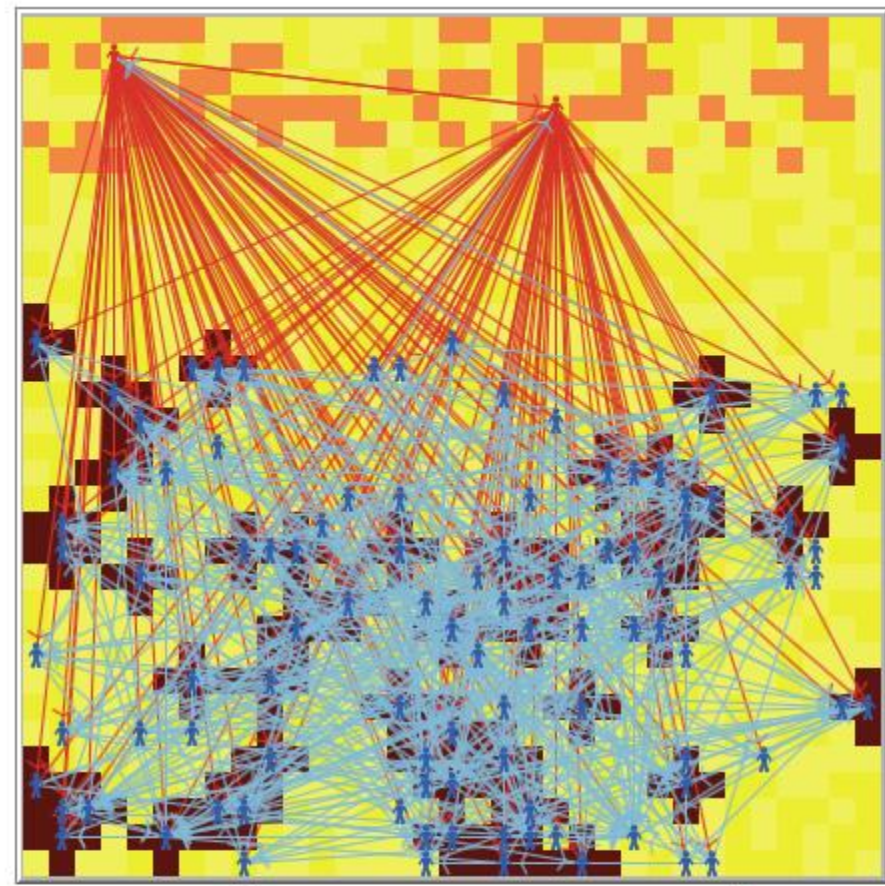
s-to-n-num-links-or-mean-exp-num-links
2

n-to-n-num-links-or-mean-exp-num-links
1

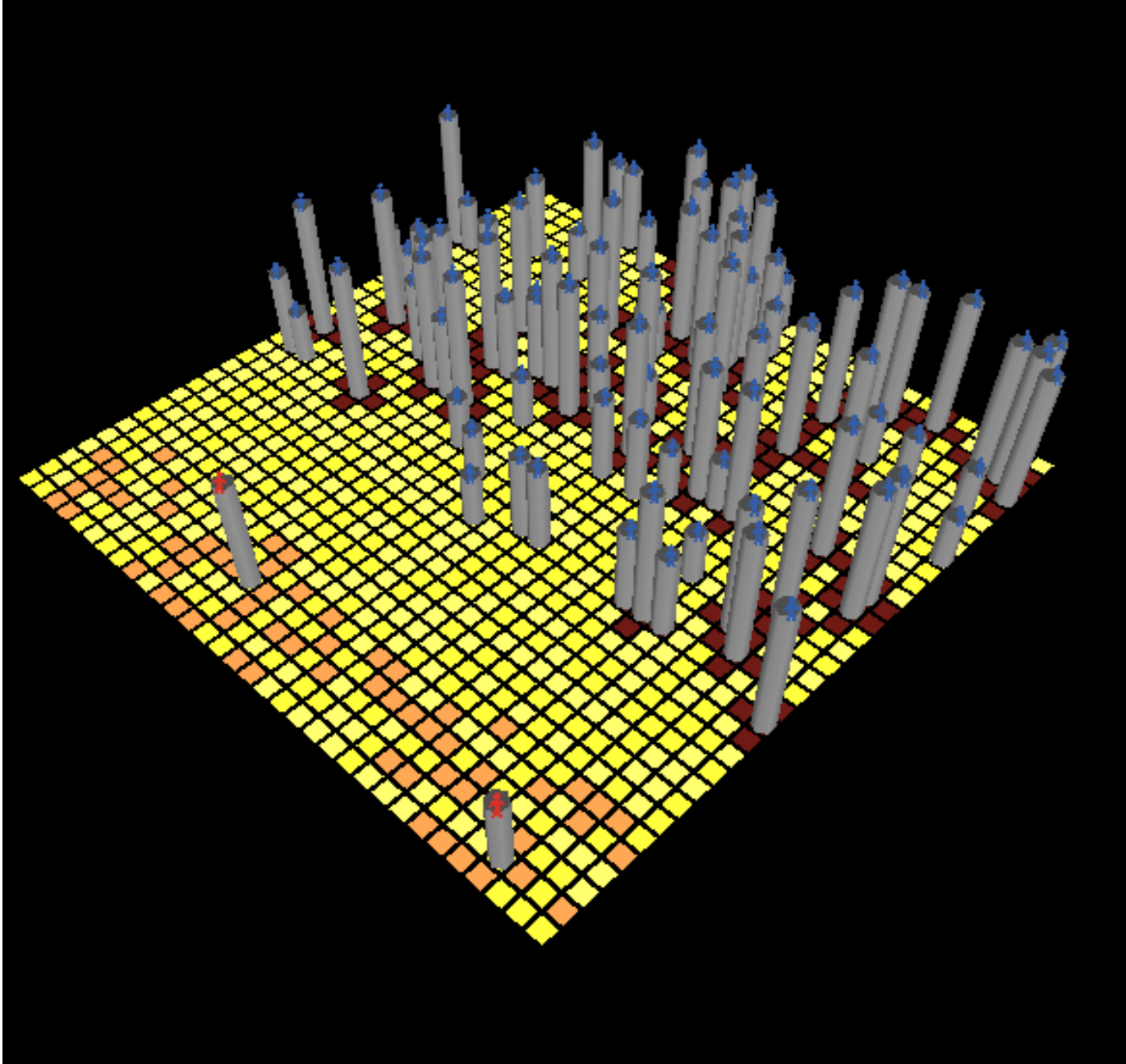
n-to-s-num-links-or-mean-exp-num-links
2

count turtles
100

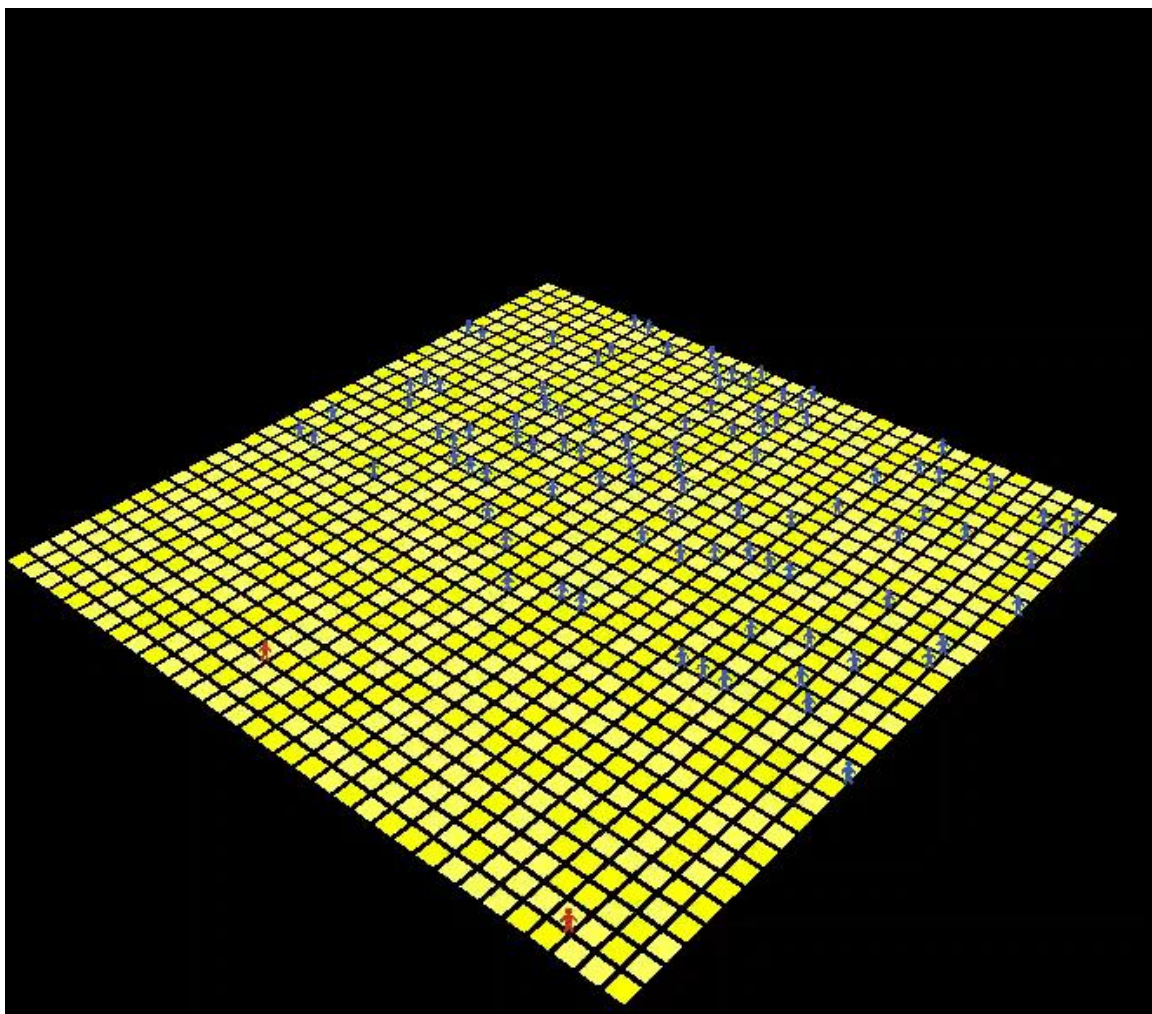
ticks
13



Large-Scale Activation
without direct stimulus
by Dispositional Contagion



Large-Scale Activation without Direct Stimulus



Toward a Theory of the First Actor

- Our Post-Doc Jeewoen Shin and I have some preliminary analytics
- And are pursuing this computationally
- But it is clearly more than an outlier of significant interest to the study of cascading social phenomena.

Inverse Generative Social Science

- Machine learning is augmenting humans, crushing them at chess, and replacing them, but it is not *explaining* them! It can be used to do that.
- Using evolutionary programming to discover ABMs that generate target macro-data.
- Typically hand-crafted, including *Agent_Zero*.
- Stipulate only minimal code components and concatenation operators (mathematical, logical) and evolve fittest AMBs.
- Data-driven evolution of generative micro-models
- “Toward Inverse Generative Social Science using Multi-Objective Genetic Programming” Vu, Probst, Epstein, et al. *GECCO* 2019.
- Founding Workshop in January 2019 Washington, DC.

- Thank you!
- Please feel free to follow up: je65@nyu.edu

- For southerners to act first:
- $dN_i + dN_{i \rightarrow N} < dS_i + dS_{i \rightarrow S}$ \Rightarrow $dN_i < dS_i$ \Rightarrow $dN_{i \rightarrow N} < dS_{i \rightarrow S}$ \Rightarrow $1 + dN_{i \rightarrow N} < dS_{i \rightarrow S}$
- $\Rightarrow 1 < dS_{i \rightarrow S} - dN_{i \rightarrow N}$ **for any pairs of northerner and southerner.**
- In other words, southerners could act first if $w_{N \rightarrow N} \downarrow, w_{N \rightarrow S} \uparrow, dN_i \downarrow, dS_i$
- In order to dS_i , there should be many northerners.
- In order to dN_i , we can disconnect graph among northerners.
- i.e., To make southerners act first, $w_{N \rightarrow N} \downarrow, w_{N \rightarrow S}$, **the number of northerners, sparse network among northerners, dense connection between northerners and southerners.**
-

Network Structure a “Poincare Map” of Continuum Affinity Dynamic

- Different Poincare Sections (Link thresholds) yield *different structure* dynamics, for *same* affinity dynamic.

Structure as Function of Threshold

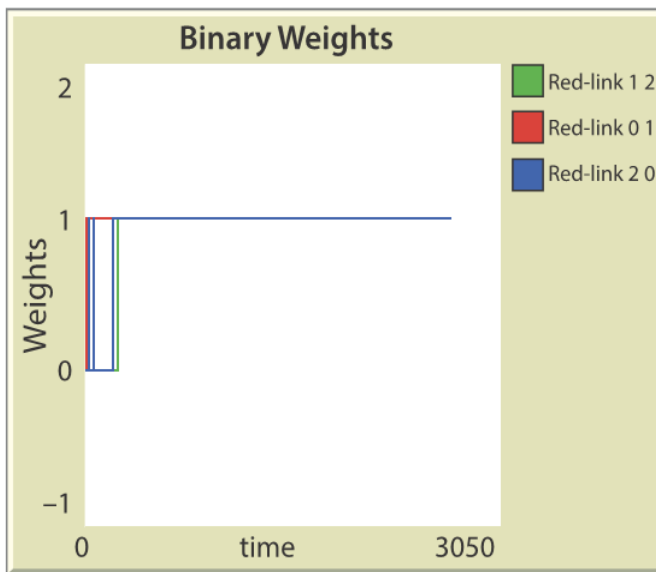


FIGURE 94. Threshold 0.25

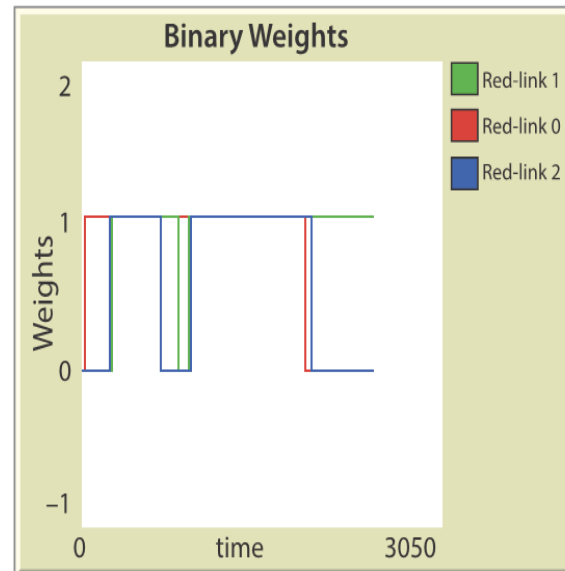


FIGURE 95. Threshold 0.5

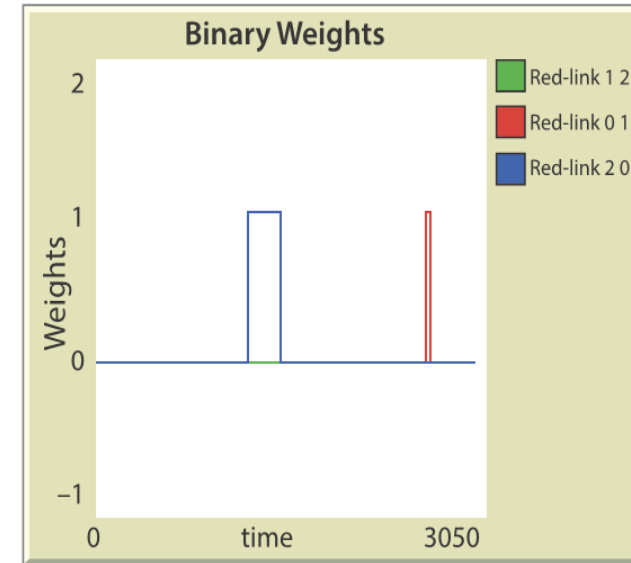
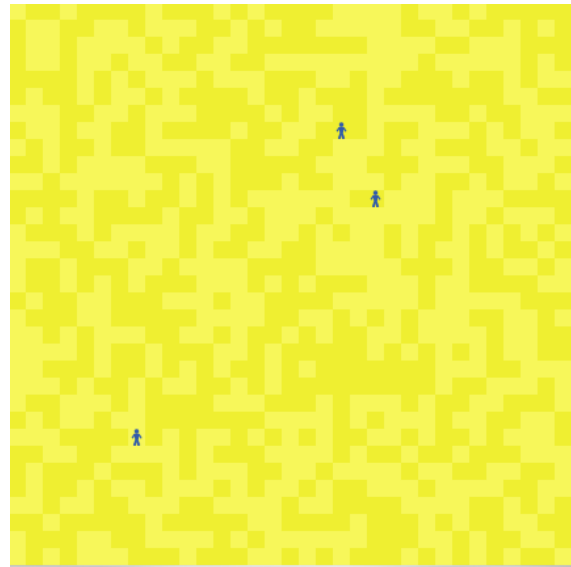


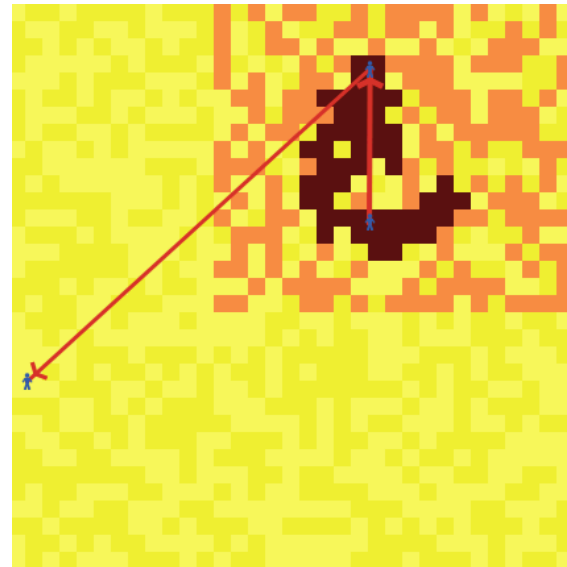
FIGURE 96. Threshold 1.0

For the same affinity dynamics, different thresholds produce different structure dynamics

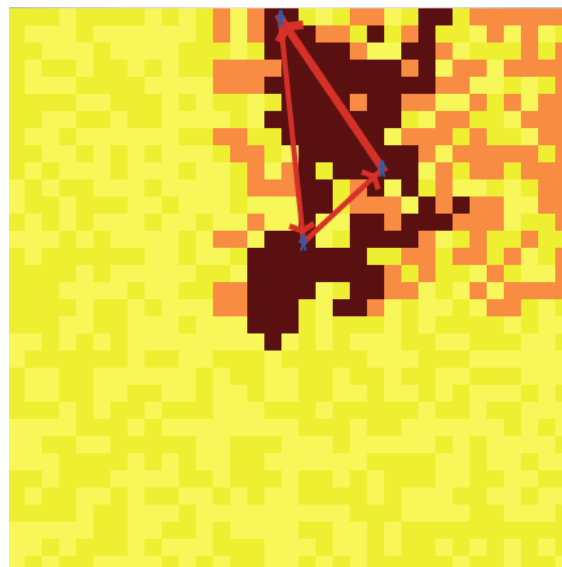
Link Formation and Breakage: Dynamics of Structure Proper



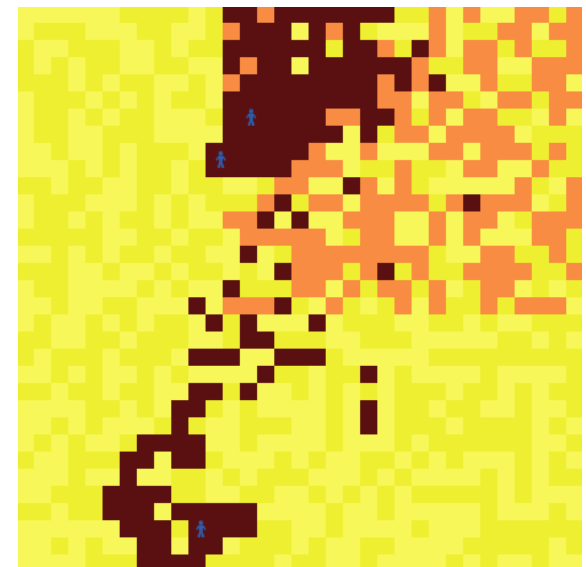
None



Partial



Full



None

Sexual networks are obviously dynamic and crucial to STD dynamics.

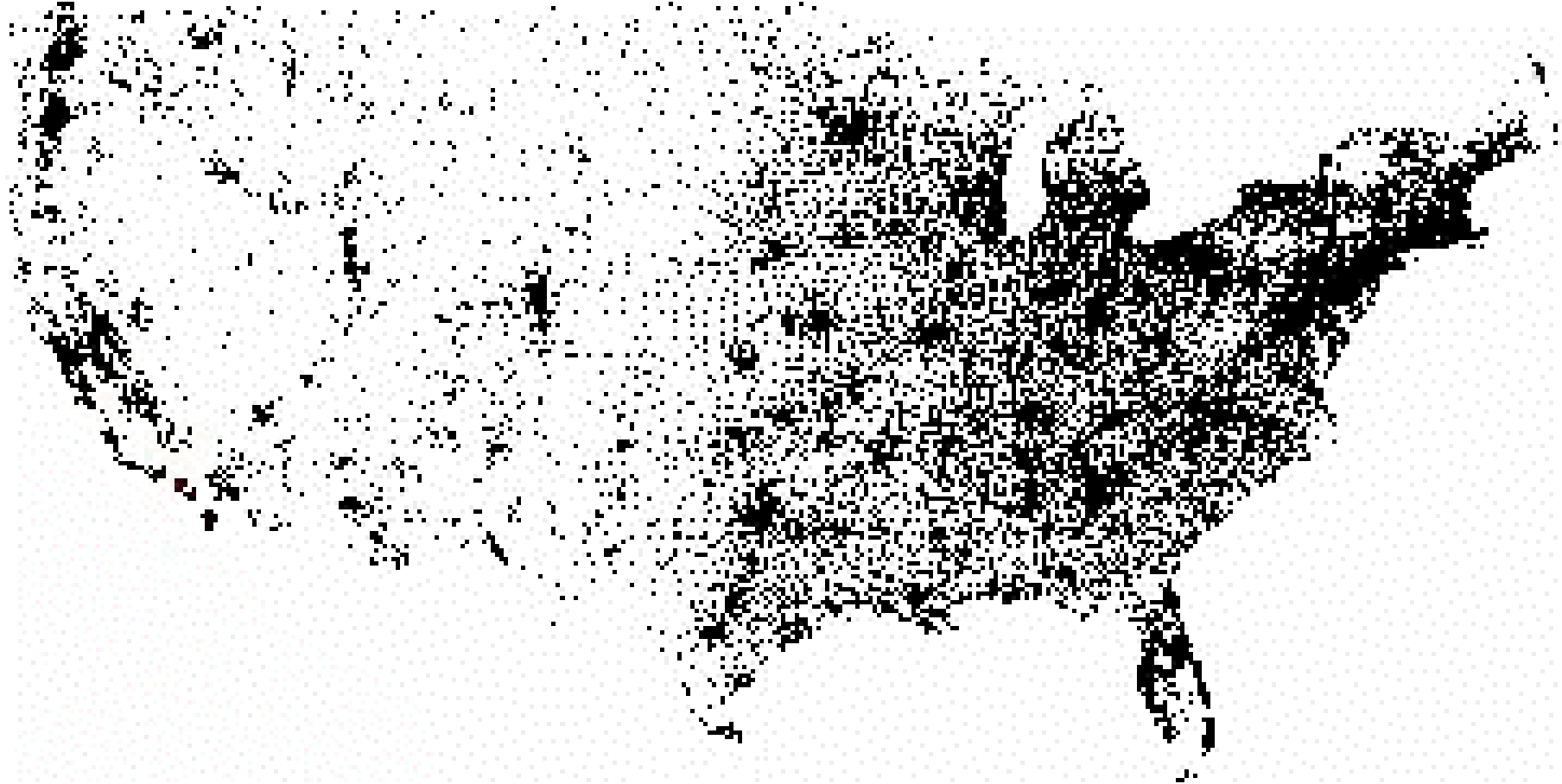
Departure From Literature

- Not preferential attachment. Long mathematical history, moderns (Barabasi and Albert, 1999)
- Rather, Attachment a function of strength and homophily—degree independent attachment
- Lazer 2001 (homophily) and Levitan and Wisser 2009 (strength)
- Testable Hypothesis

Scale up Dramatically and Populate Large Models

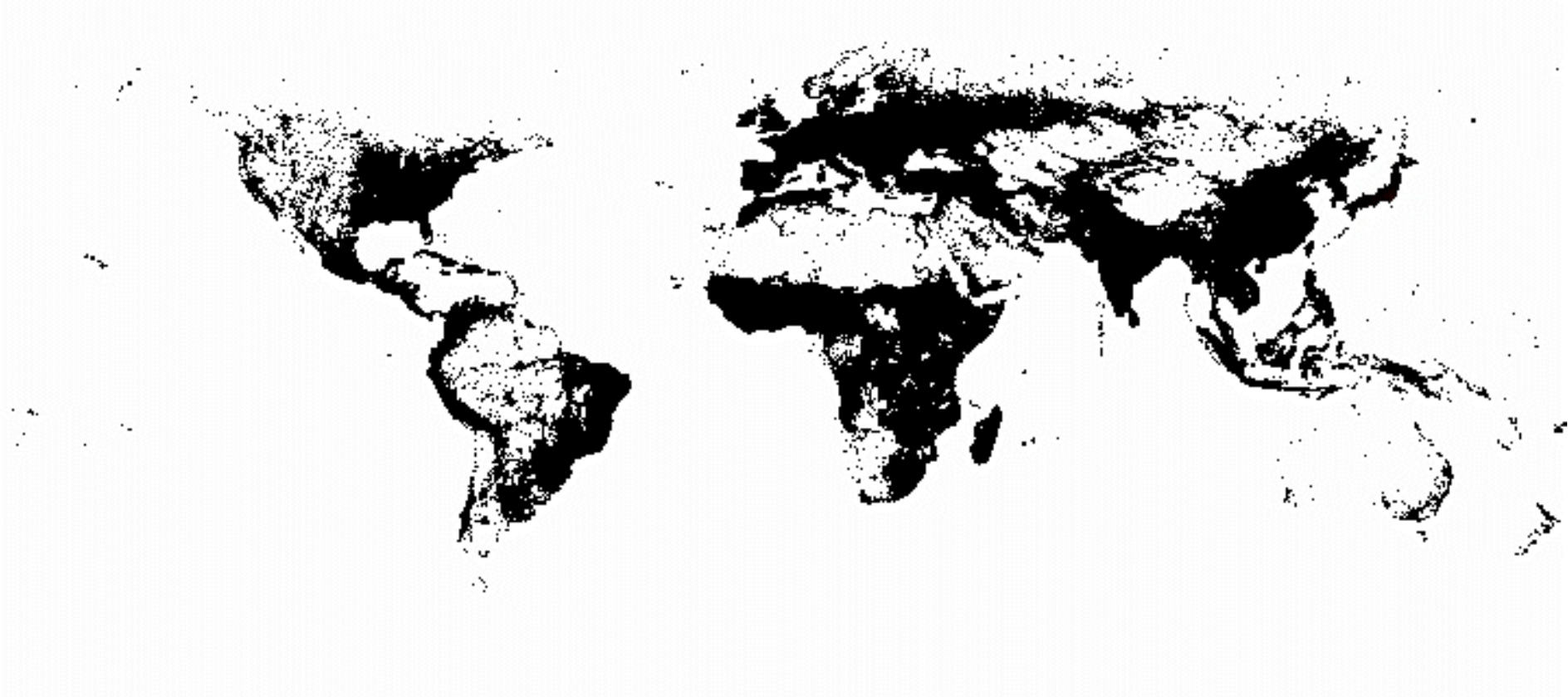
- Have the capacity to do entire economies and linkages

US National Model



Parker, J. and Epstein, J.M., 2011. A distributed platform for global-scale agent-based models of disease transmission. *ACM Transactions on Modeling and Computer Simulation (TOMACS)*, 22(1), p.2.

Global-Scale Infectious Disease Model



Epstein, J.M., 2009. Modelling to contain pandemics. *Nature*, 460(7256), p.687.

Parker, J. and Epstein, J.M., 2011. A distributed platform for global-scale agent-based models of disease transmission. *ACM Transactions on Modeling and Computer Simulation (TOMACS)*, 22(1), p.2.

- Thank you!
- Please feel free to follow up: je65@nyu.edu